

Modélisation numérique des problèmes de l'ingénieur



CALCUL ELMENTS FINIS ET OPTIMISATION DE FORME DANS LES STRUCTURES AEROSPATIALES



**Pr. BOUDI El Mostapha
Ecole Mohammadia d'Ingénieurs
Rabat**



En quelques mots ...

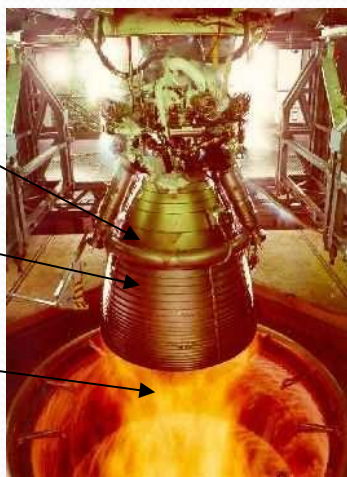
Objectif : Contrôle des calculs par la Méthode des éléments
Finis

Fournir des outils dédiés pour la résolution informatique des
phénomènes physiques et Optimiser la forme des pièces
Mécaniques (Légèreté / Résistance)

Structure

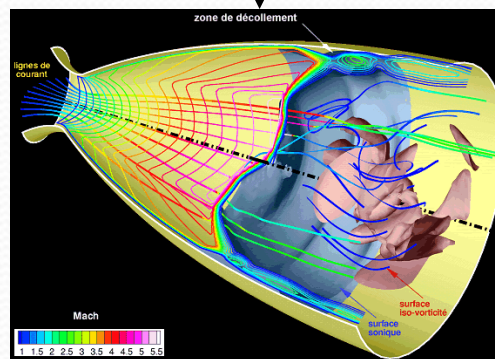
Thermique

Fluide



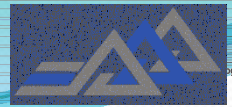
Source : technoscience

Modèle réel



Source : ONERA

Modèle numérique



Intérêts « industriels »



www.dt.insu.cnrs.fr

**Aéronautique/ Aérospatial
Vibration - acoustique**



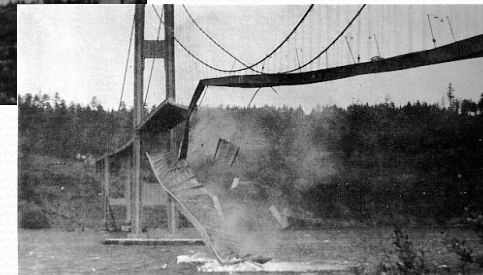
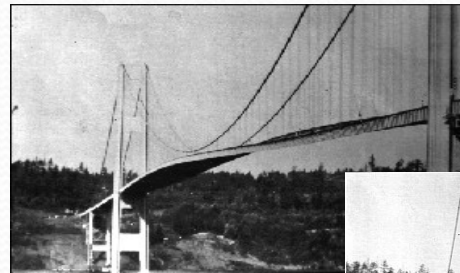
www.otua.org/acier/seisme/

Protection séisme



www.cnes.fr

Couplage fluide-structure

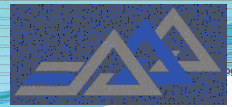


«Tacoma narrows bridge »

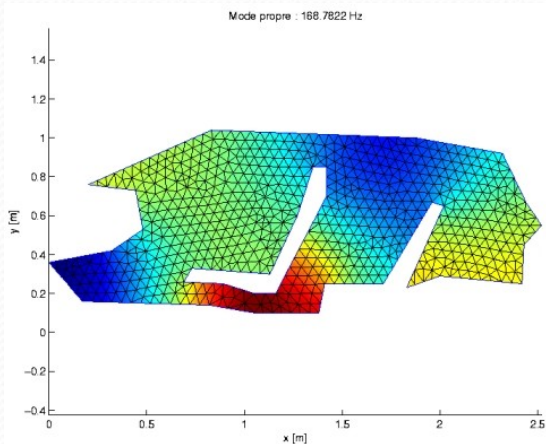
Ouvrage génie civil

...

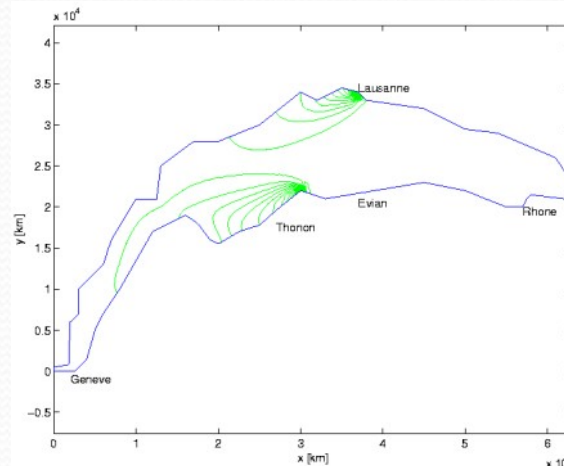
Pourquoi EF?



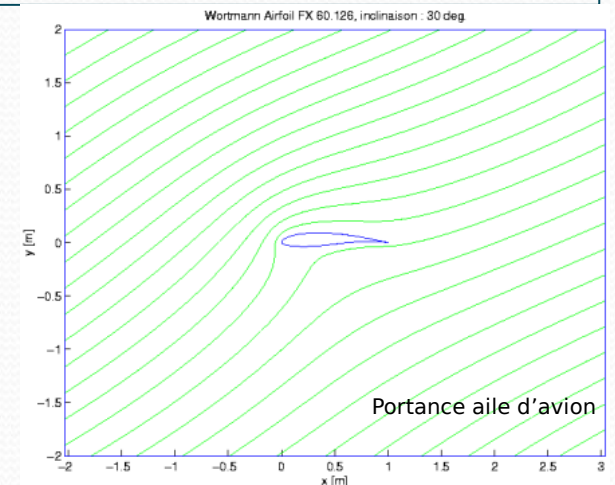
- Passage incontournable dans la boucle de conception d'un produit industriel
 - Automobile, aéronautique, acoustique, génie civil ...
 - Un ingénieur sur Trois concerné par le numérique
- 99 % de la physique sous la forme d'E.D.P.
- « Outils » mathématiques classiques (fondamentales) valables pour moins de 1 % des cas !!



Acoustique automobile



Pollution d'un lac





Bagages nécessaires ...

- **Mathématique** :
 - Équations différentielles ordinaires
 - Techniques d'intégration standard
 - Opérations matricielles de base
 - Notion d'interpolation
 - Interpolations (Courbes, Surfaces, Topologie,...)
- **Physique** : ?
- **Ingénieur** : développer le bon Sens et un esprit critique
- **Informatique** : (C++, Fortran, Matlab, ...)

Complexité : Multi compétences

Intérieur:

- Capacité transport
- Confort passagers
- ...

Fluide:

- Aérodynamique
- Traînée
- Acoustique
- ...



Structure:

- Tenue
- Fatigue
- Aéroélasticité
- Fréquences
- ...

Moteurs:

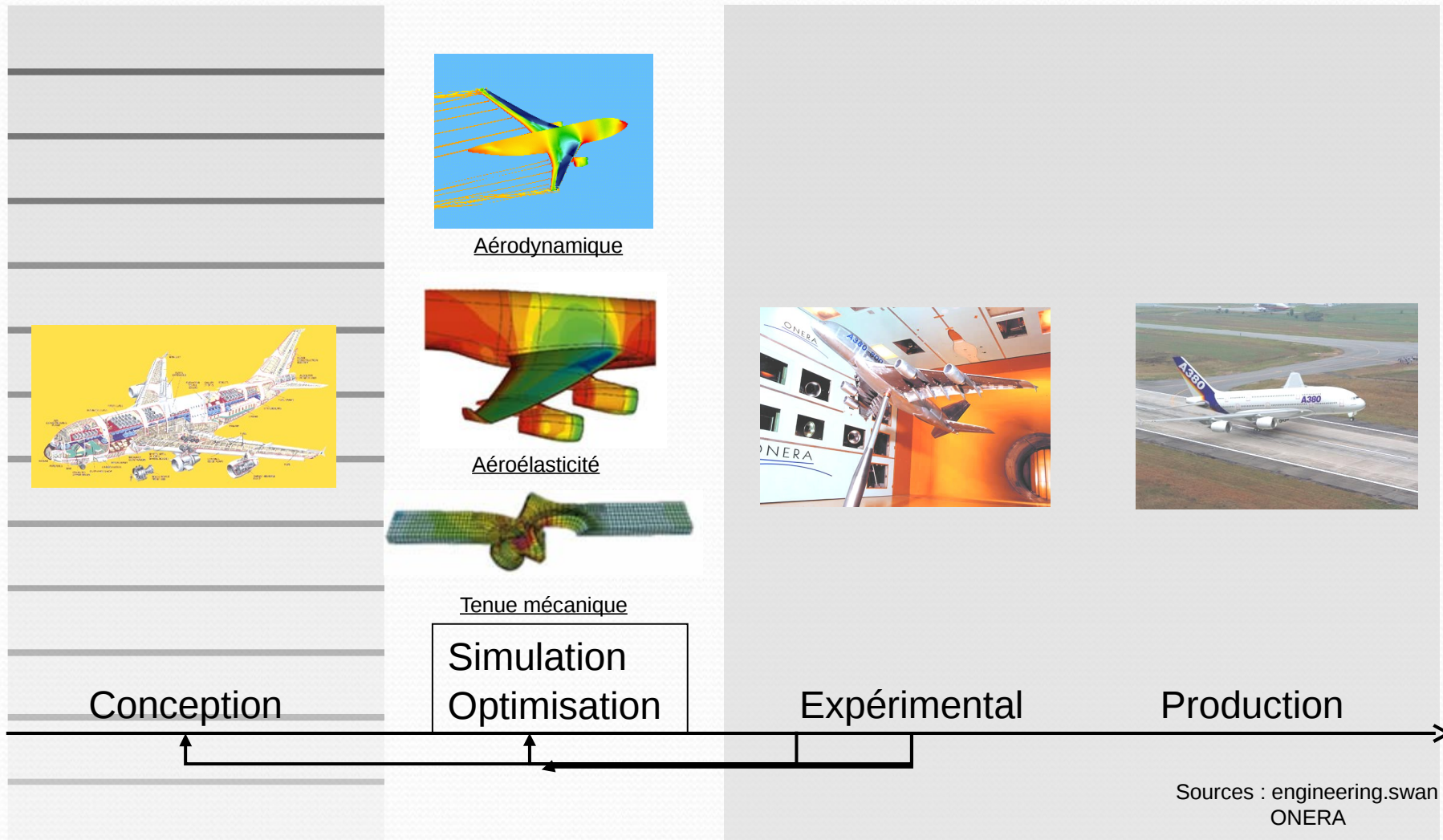
- Combustion
- Poussée
- Acoustique environnementale
- ...

Electronique / Automatisme:

- Automatisme
- Contrôle
- Asservissement
- Commandes
- ...

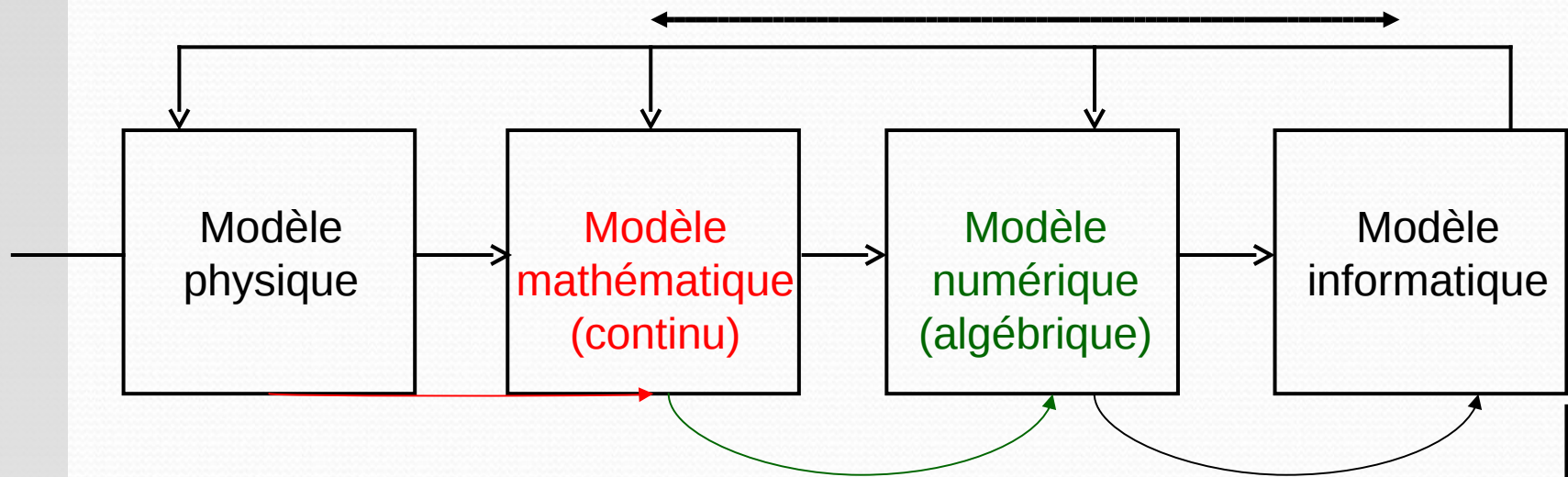
Source : futura-sciences

Chaîne de conception « industrielle »



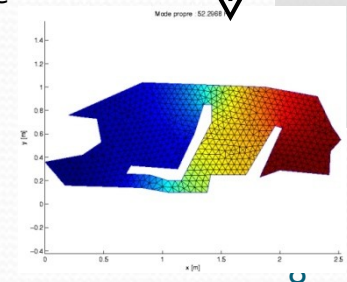
« Boucle de Modélisation »

Démarche en 4 étapes (ou modèles) distinctes :
EF



Sources d'erreurs

$$= \text{Écart entre solution réelle et solution exacte du problème mathématique} + \text{Écart entre solution exacte du problème mathématique et solution du système discret} + \text{Écart entre solution exacte du système discret et solution informatique}$$

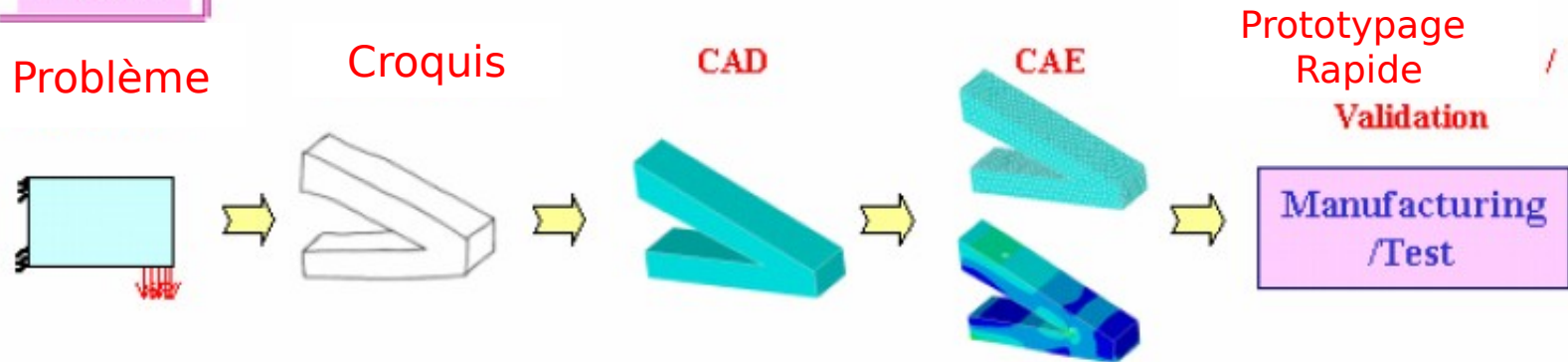




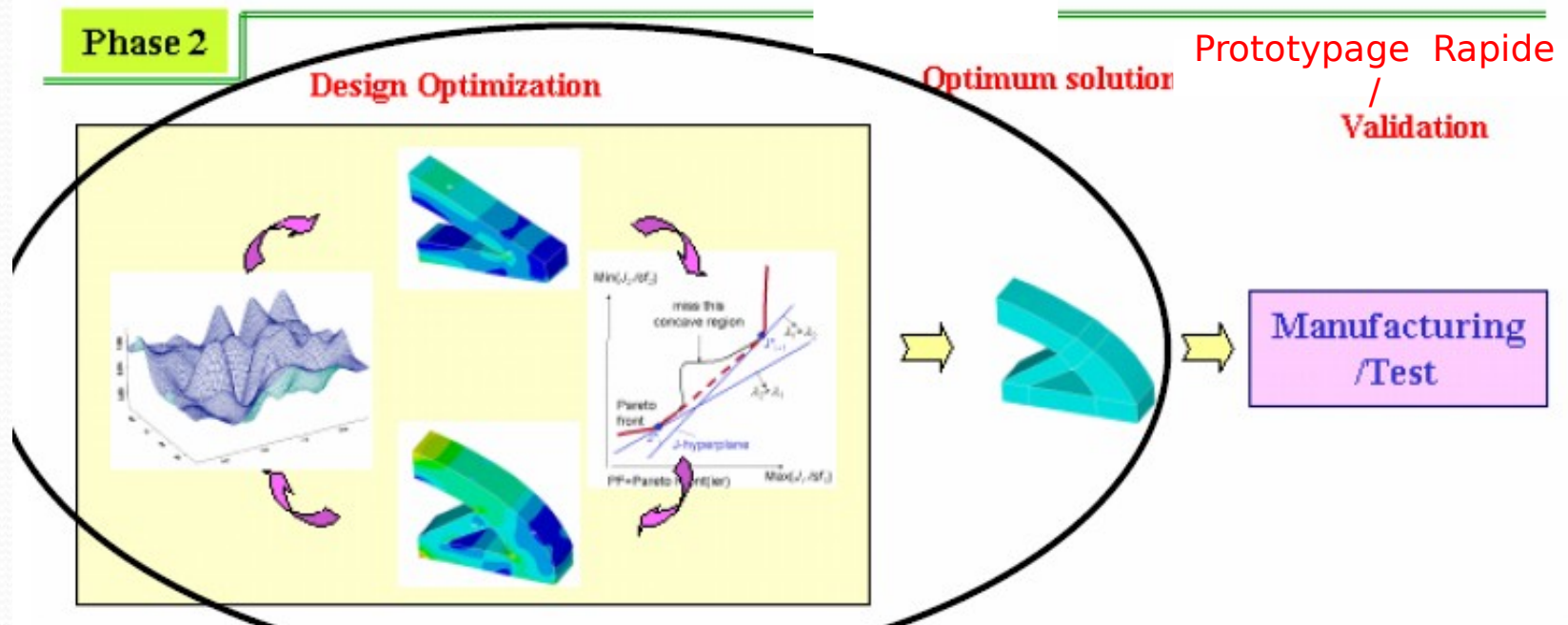
OPTIMISATION DES STRUCTURES AEROSPATIALES

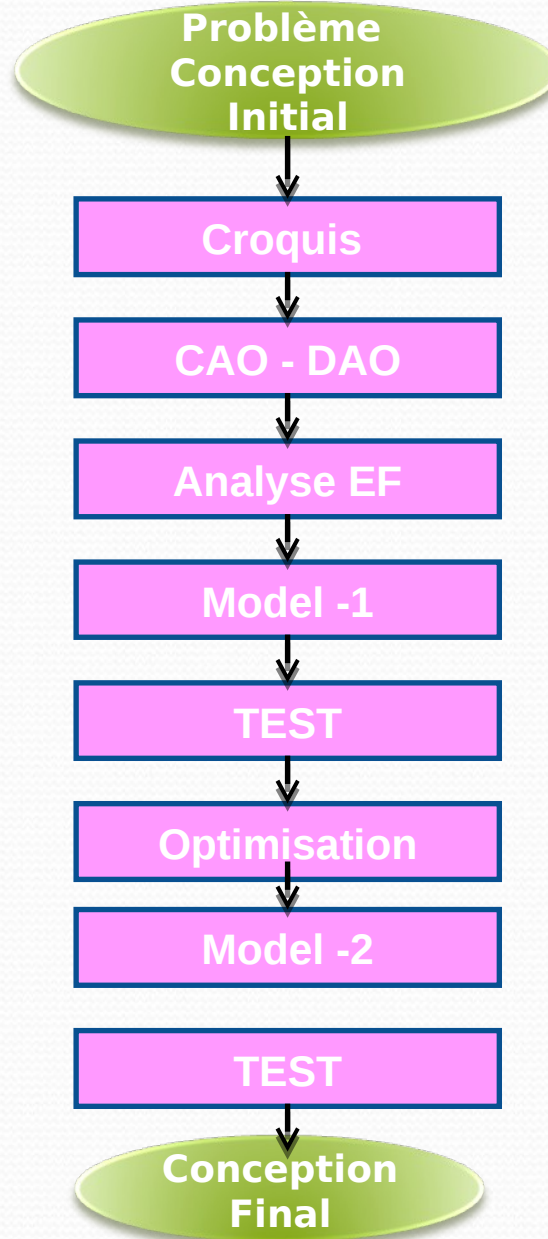
PHASES D'OPTIMISATION

Phase 1



Phase 2







PHASES D'OPTIMISATION

QUESTIONS : Quelle est la meilleure Conception « Meilleur Design » ?

- 1- Quel est le critère de choix de la meilleure conception →
Fonction Objectif**
- 2- Principes → Contraintes, Spécifications techniques**
- 3- Comment décrire les différentes conceptions →
Variables de conception**



Minimize $f(\mathbf{x})$

Subject to $g(\mathbf{x}) \leq 0$

$h(\mathbf{x}) = 0$



CONTRAINTES

2. Requirements

Manufacturing Cost (C): $C \leq 3.6\$ /part$

Performance (δ_1, δ_2, f_1):
Displacement $\delta_1 \leq 0.078$ mm
Displacement $\delta_2 \leq 0.012$ mm
First natural frequency $f_1 \geq 195$ Hz

Mass (m): $m \leq 0.27$ lbs

Surface Quality (Q): $Q \geq 2$

Load Case (F): $F1 = 50$ lbs / $F2 = 50$ lbs / $F3 = 100$ lbs

The part has to conform to the interface requirements and geometrical boundary conditions shown on page 2 of this document. This requirement cannot be waived.

3. Priorities

Low manufacturing cost is the first priority for this product. Next, the customer cares about light-weighting (low mass) and thirdly, structural performance should be as high as possible. These priorities are shown in the Ishii-matrix below:

Attribute	Constrain	Optimize	Accept
Cost	■		
Performance			■
Mass		■	

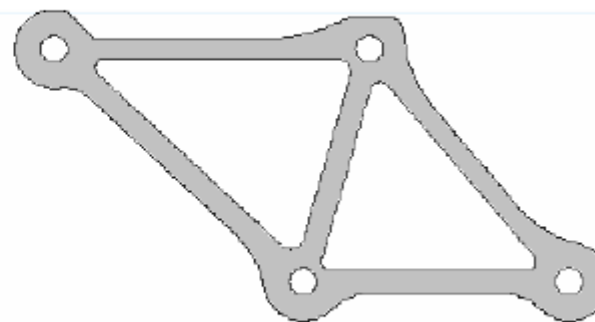
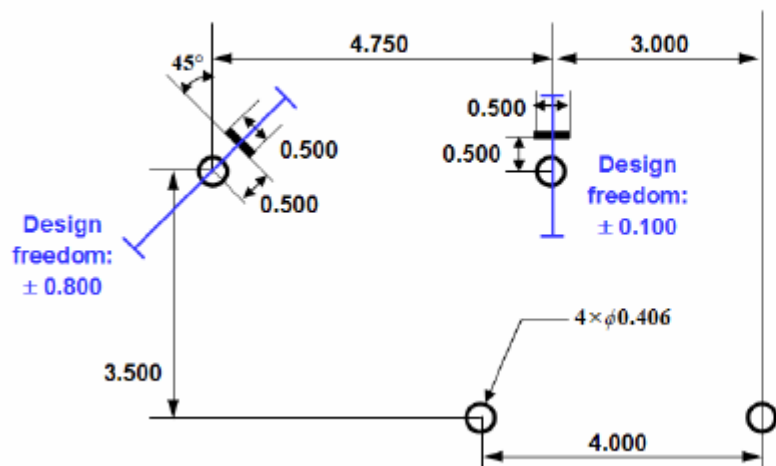
**Contraintes
Qualitatives**

**Contraintes
Quantitatives
Fonction
Objectifs**

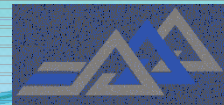
VARIABLES DE CONCEPTION

PARAMETRES CHOISIS POUR DEFINIR LA CONCEPTION

Variables de conception contrôlés par le concepteur



Ici la position et diamètres des trous



For computational design optimization,

➔ **Objective function and constraints must be expressed as a function of design variables (or design vector \mathbf{X})**

Objective function: $f(\mathbf{x})$

Constraints: $g(\mathbf{x}), h(\mathbf{x})$

Cost = $f(\text{design})$

Displacement = $f(\text{design})$

Natural frequency = $f(\text{design})$

Mass = $f(\text{design})$

What is "f" for each case?



Minimize $f(\mathbf{x})$

Subject to $g(\mathbf{x}) \leq 0$

$h(\mathbf{x}) = 0$

$f(\mathbf{x})$: Objective function to be minimized

$g(\mathbf{x})$: Inequality constraints

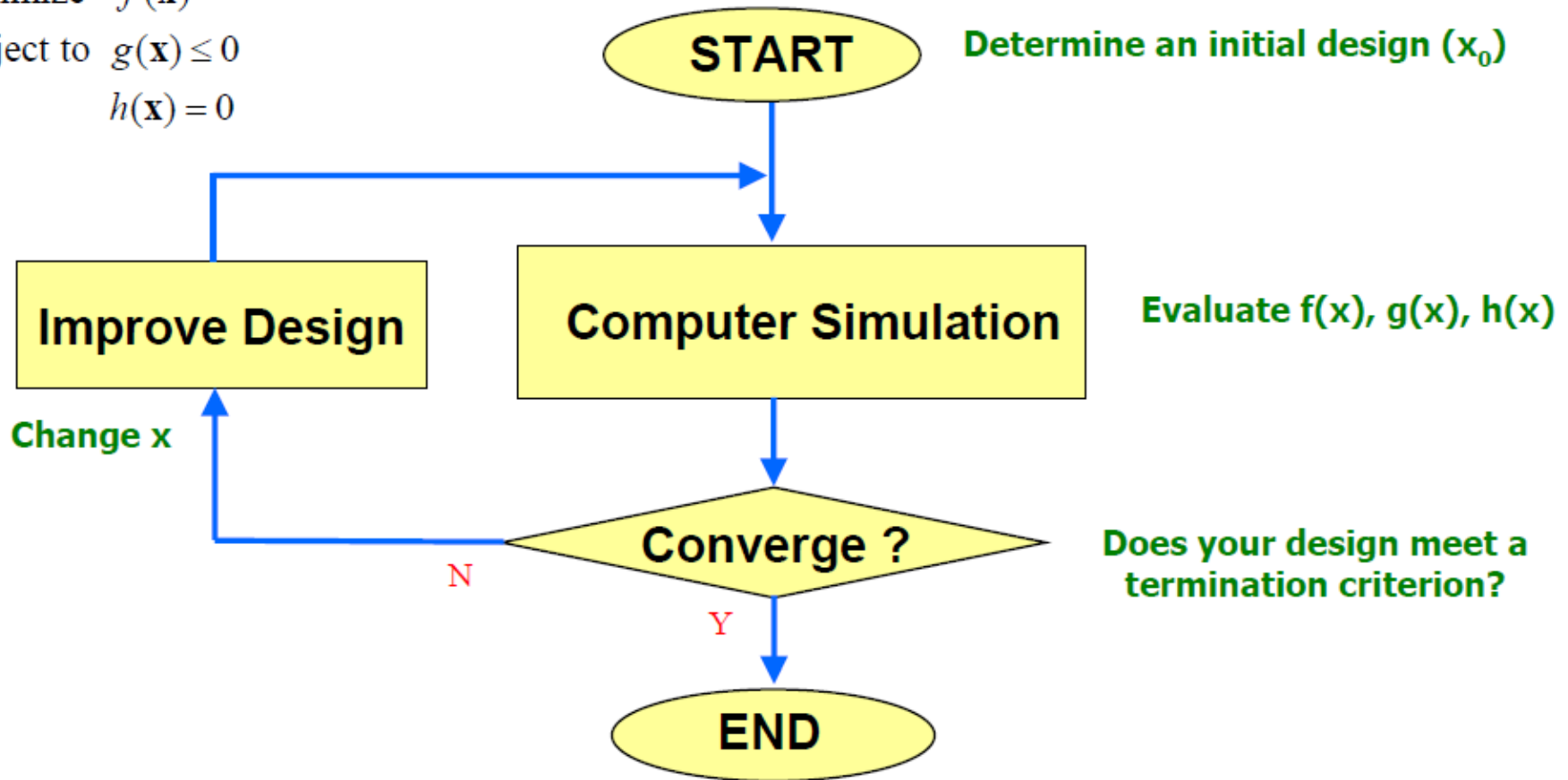
$h(\mathbf{x})$: Equality constraints

\mathbf{x} : Design variables



PROCEDURE D'OPTIMISATION

Minimize $f(\mathbf{x})$
Subject to $g(\mathbf{x}) \leq 0$
 $h(\mathbf{x}) = 0$





Selecting the best "structural" design

- Size Optimization
- Shape Optimization
- Topology Optimization

OPTIMISATION STRUCTURELLE

$$\begin{aligned} &\text{minimize } f(\mathbf{x}) \\ &\text{subject to } g(\mathbf{x}) \leq 0 \\ &\quad \quad \quad h(\mathbf{x}) = 0 \end{aligned}$$



BC's are given



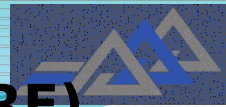
Loads are given

1. To make the structure strong
e.g. Minimize displacement at the tip

➡ $Min. f(\mathbf{x})$

2. Total mass $\leq M_c$

➡ $g(\mathbf{x}) \leq 0$

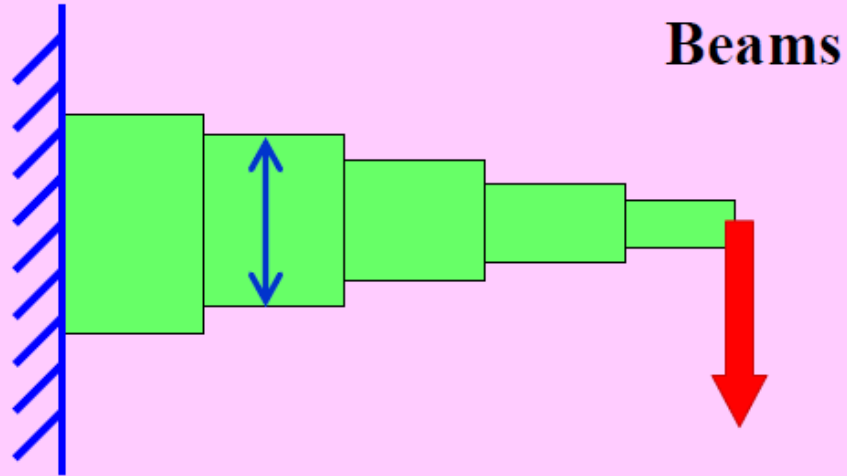


OPTIMISATION DE FORME (TAILLE DE LA STRUCTURE)

minimize $f(\mathbf{x})$

subject to $g(\mathbf{x}) \leq 0$

$h(\mathbf{x}) = 0$



Design variables (\mathbf{x})

\mathbf{x} : thickness of each beam

$f(\mathbf{x})$: compliance

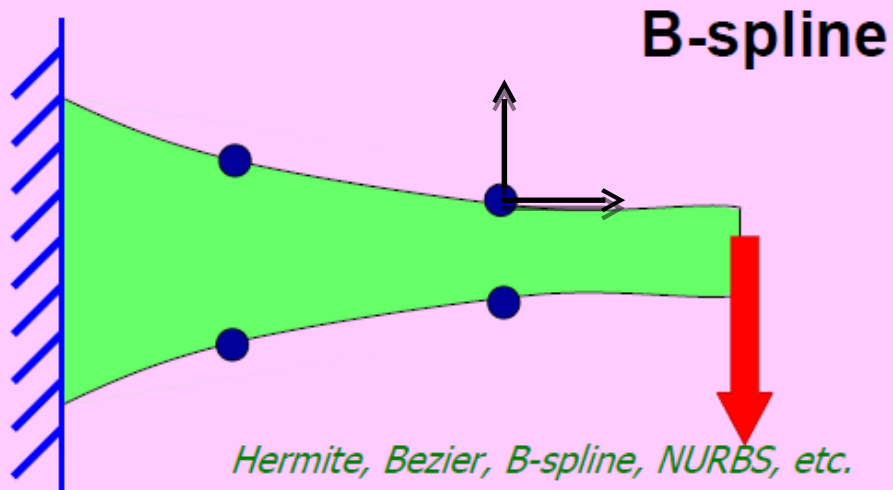
$g(\mathbf{x})$: mass

Number of design variables (ndv)

ndv = 5

OPTIMISATION DE FORME (FORME DE LA STRUCTURE)

$$\begin{aligned} &\text{minimize } f(\mathbf{x}) \\ &\text{subject to } g(\mathbf{x}) \leq 0 \\ &\quad h(\mathbf{x}) = 0 \end{aligned}$$



Design variables (\mathbf{x})

\mathbf{x} : control points of the B-spline
(position of each control point)

$f(\mathbf{x})$: compliance

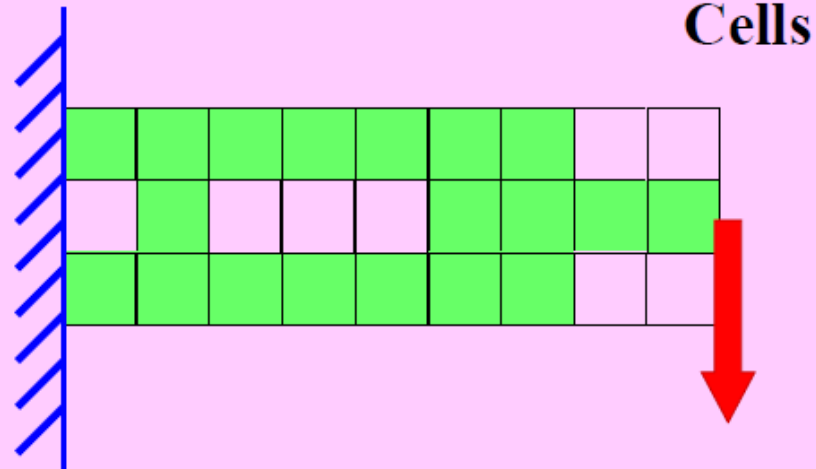
$g(\mathbf{x})$: mass

Number of design variables (ndv)

$$\text{ndv} = 8$$

OPTIMISATION TOPOLOGIQUE

$$\begin{aligned} &\text{minimize } f(\mathbf{x}) \\ &\text{subject to } g(\mathbf{x}) \leq 0 \\ &\quad \quad \quad h(\mathbf{x}) = 0 \end{aligned}$$



Design variables (x)

x : density of each cell

Number of design variables (ndv)

ndv = 27

$f(x)$: compliance

$g(x)$: mass

OPTIMISATION DE FORME (FORME DE LA STRUCTURE)

Multiobjective & Multidisciplinary Shape Optimization

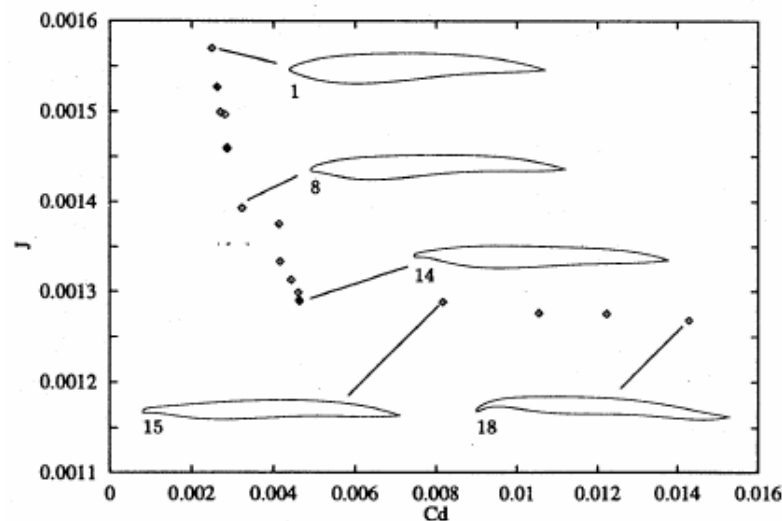
Objective function

1. Drag coefficient,
2. Amplitude of backscattered wave

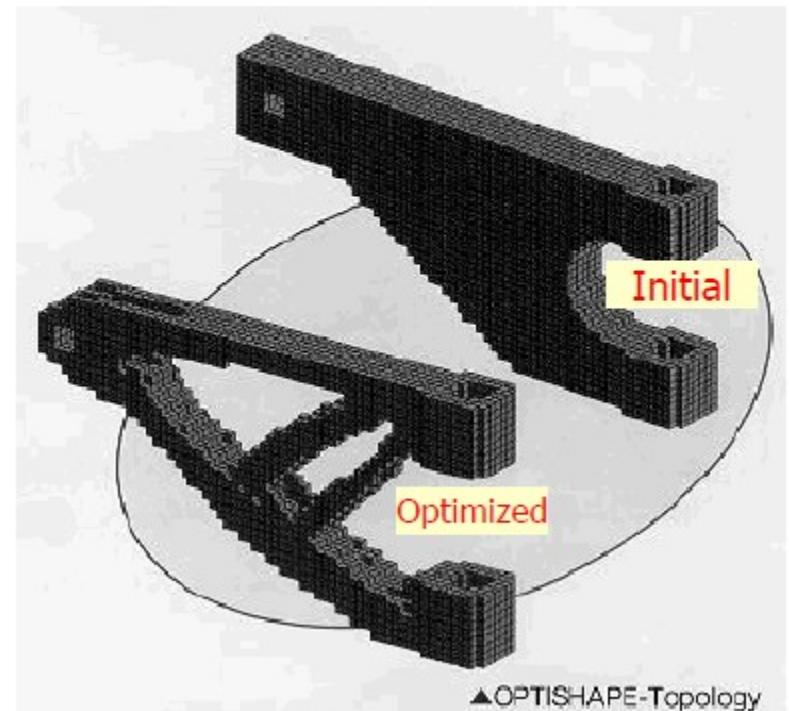
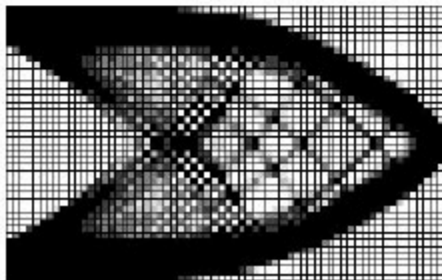
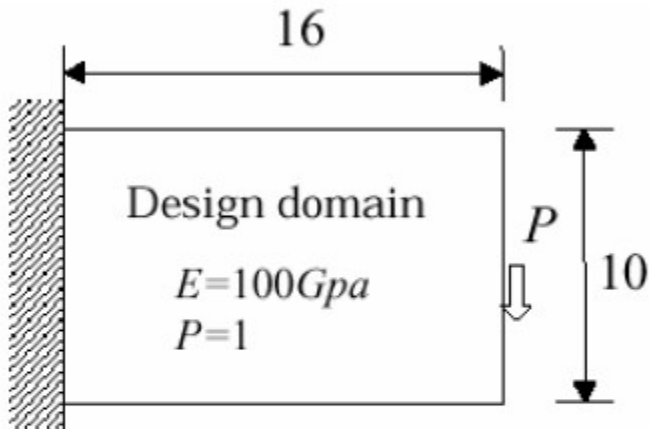
Analysis

1. Computational Fluid Dynamics Analysis
2. Computational Electromagnetic Wave Field Analysis

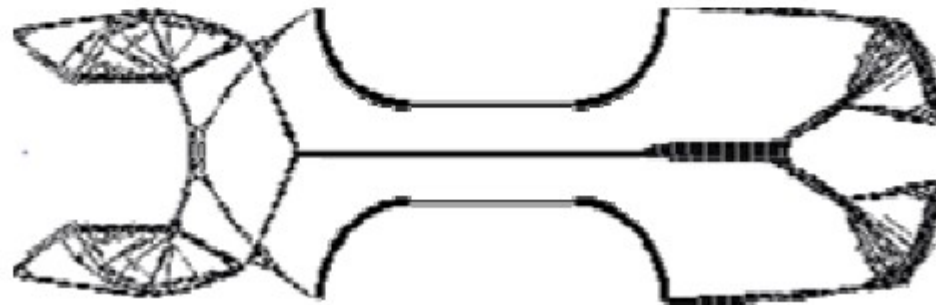
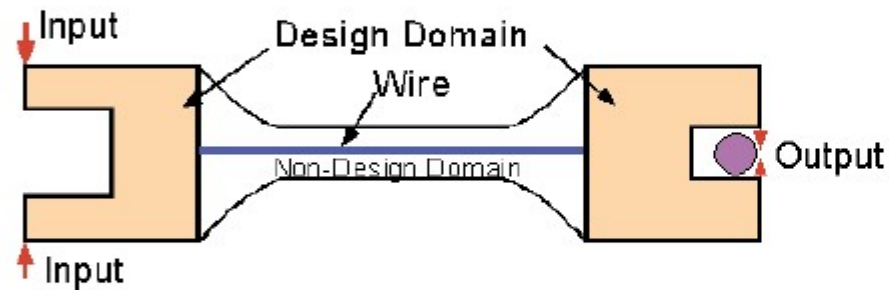
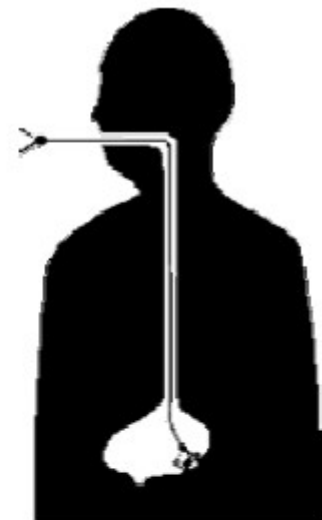
Obtain Pareto Front



Short Cantilever problem

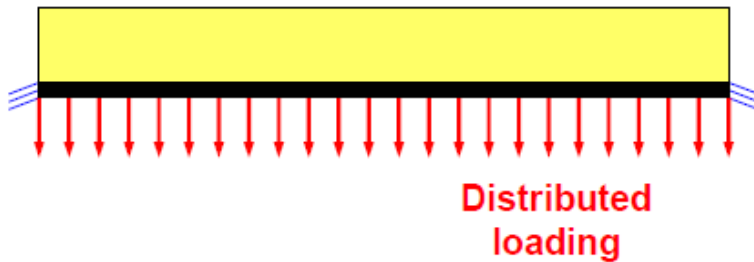


OPTIMISATION TOPOLOGIQUE



OPTIMISATION TOPOLOGIQUE

Bridge problem

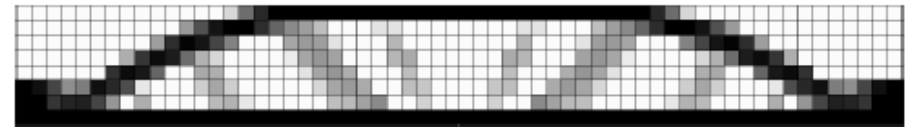


$$\text{Minimize } \int_{\Gamma} F^i z^i d\Gamma,$$

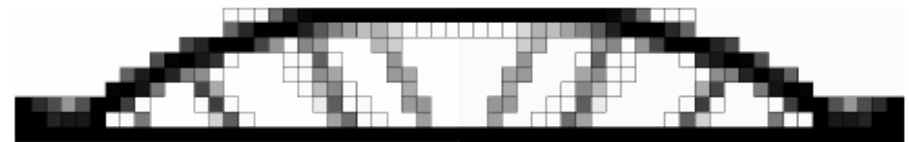
$$\text{Subject to } \int_{\Omega} \rho(x) d\Omega \leq M_o,$$

$$0 \leq \rho(x) \leq 1$$

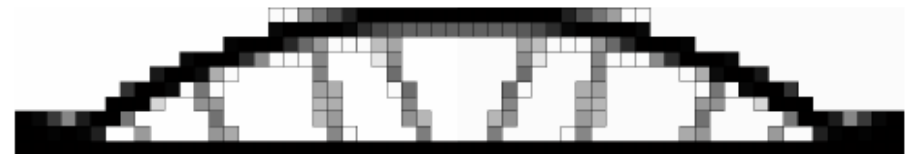
Mass constraints: 35%



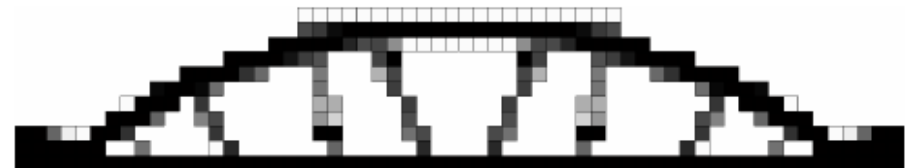
$$\text{Obj} = 4.16 \times 10^5$$



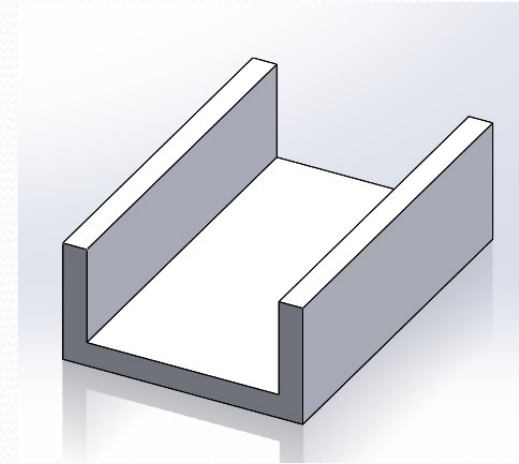
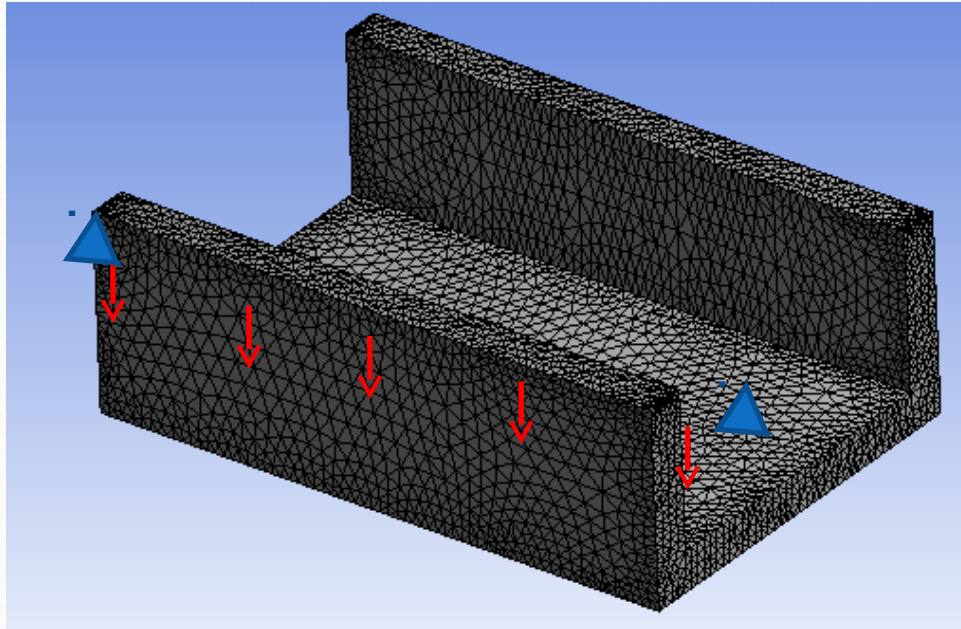
$$\text{Obj} = 3.29 \times 10^5$$



$$\text{Obj} = 2.88 \times 10^5$$



$$\text{Obj} = 2.73 \times 10^5$$



A: Optimisation de forme

Optimiseur de forme

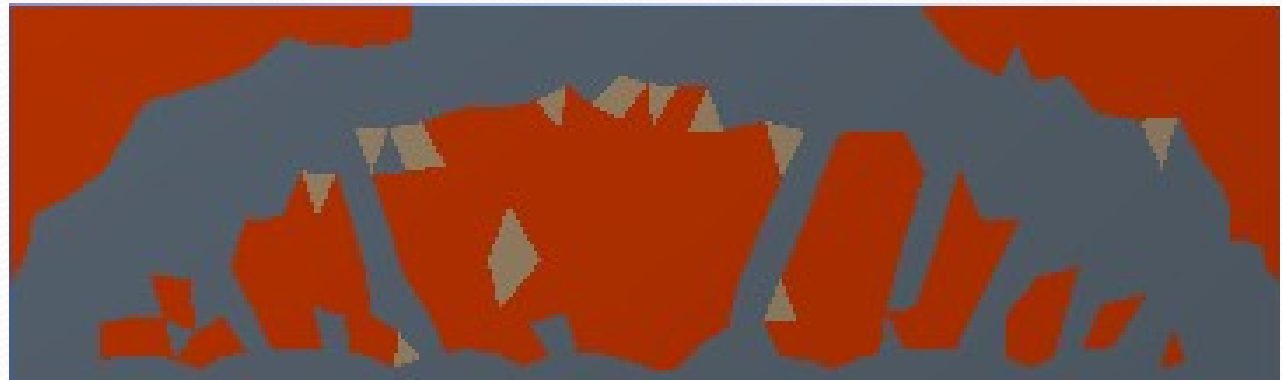
Type: Optimiseur de forme

Unité: t

Temps: 0

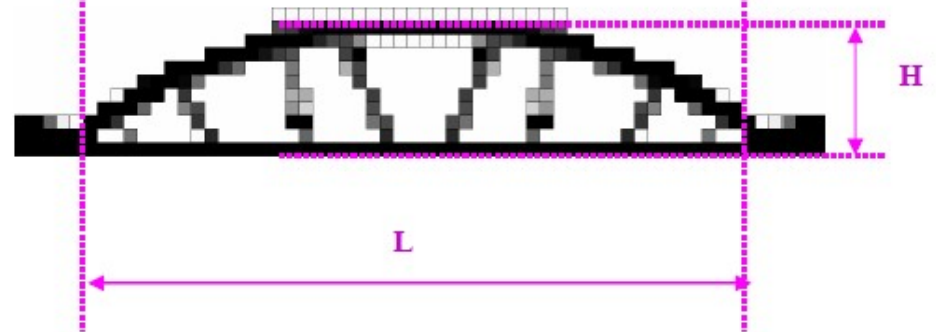
22/04/2015 23:59

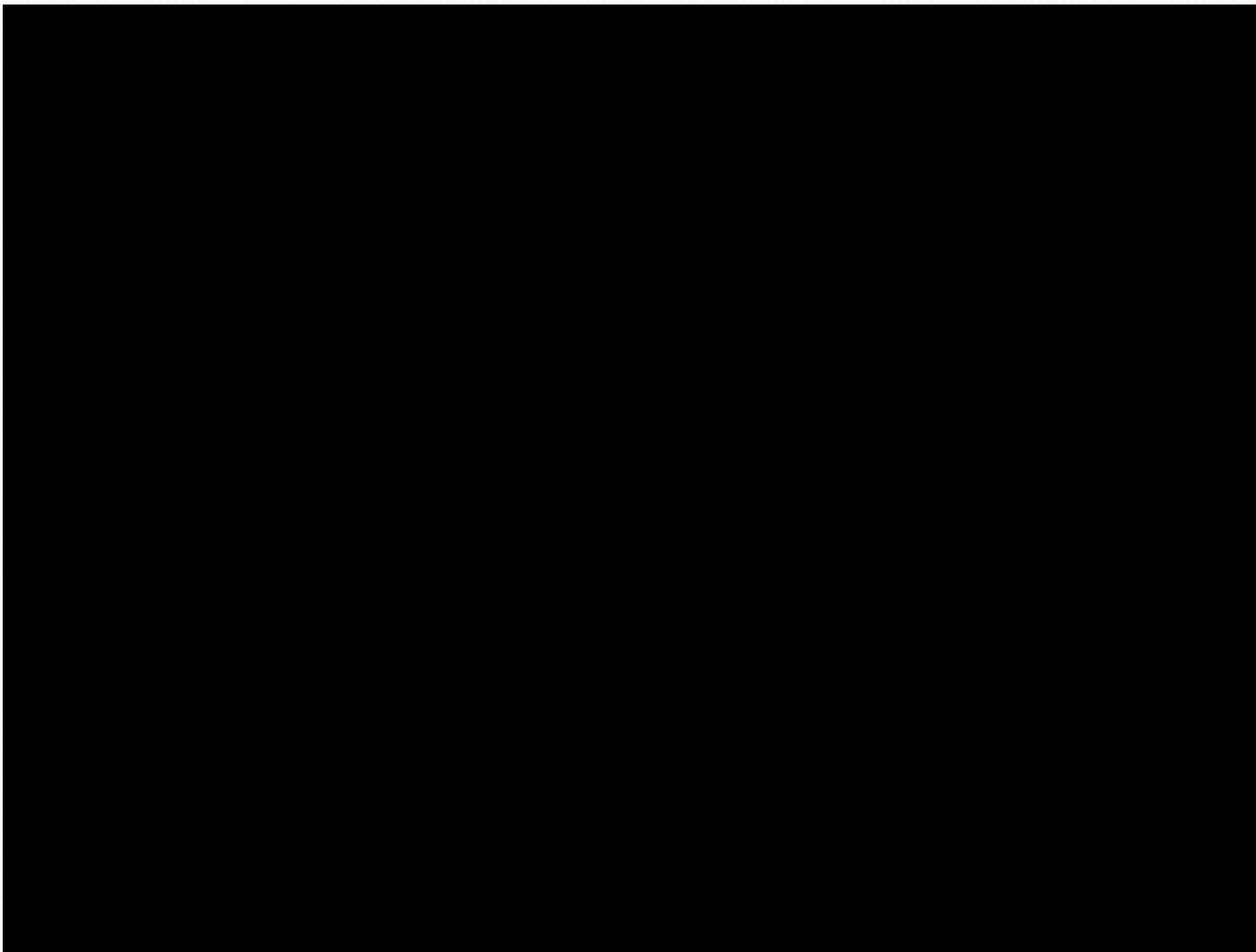
-  Retirer
-  Incertain
-  A garder



OPTIMISATION TOPOLOGIQUE

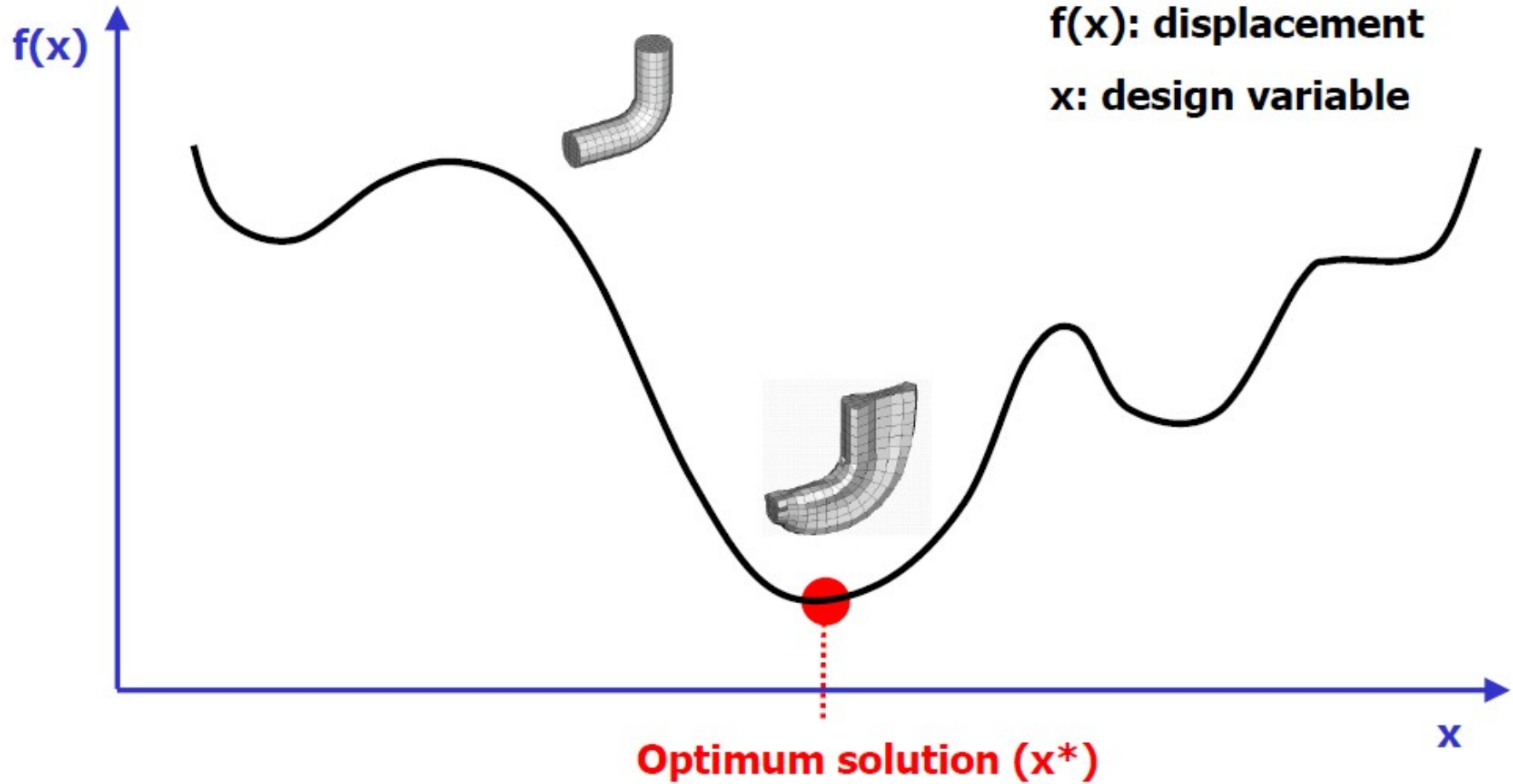
Ex : PONT





OPTIMISATION STRUCTURELLE : Représentation Graphique

SOLUTION OPTIMALE

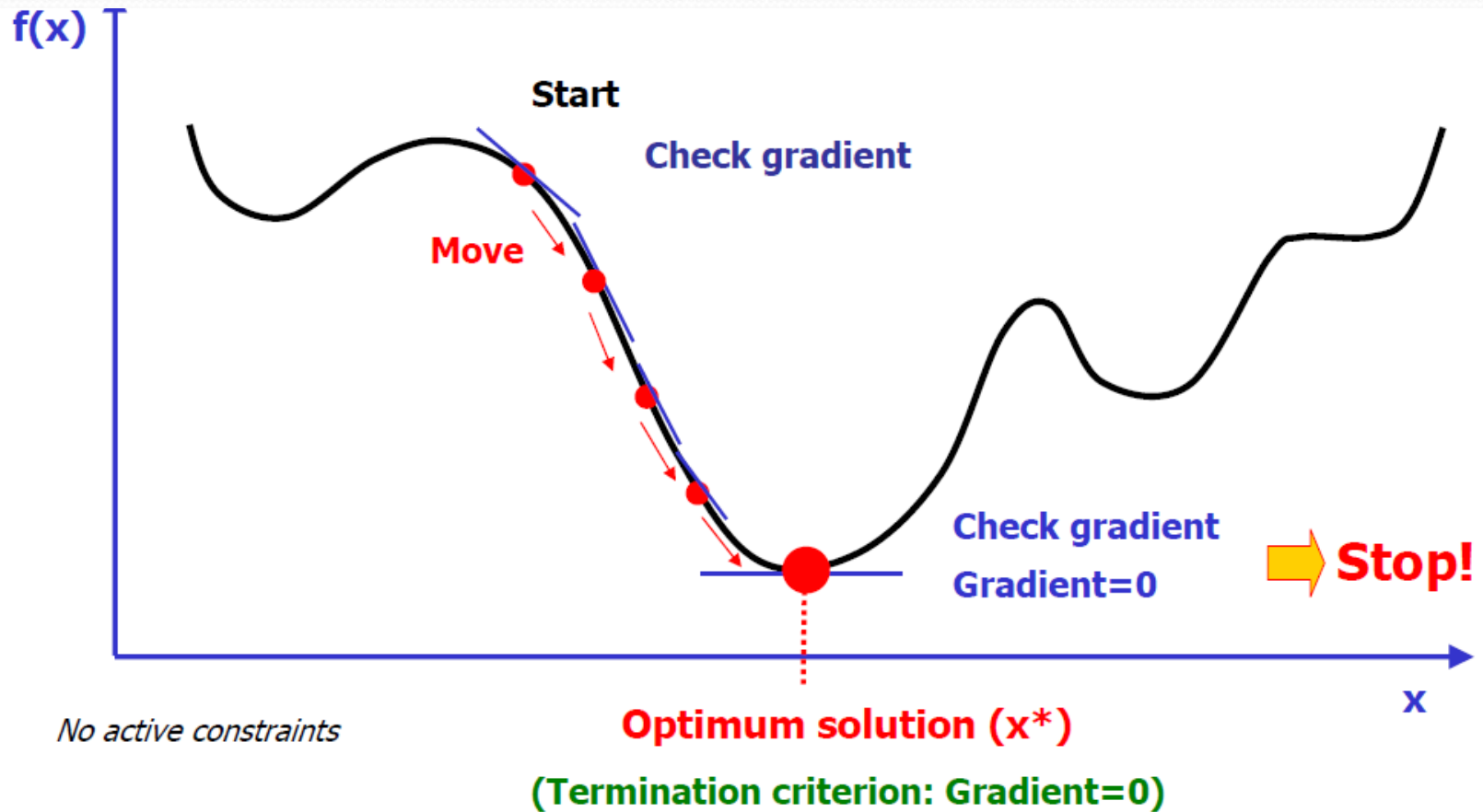




Deux Méthodes d'optimisation :

- Méthodes basées sur le Gradient**
- Méthodes Heuristics**

METHODES D'OPTIMISATION : METHODES BASEES SUR LE GRADIENT

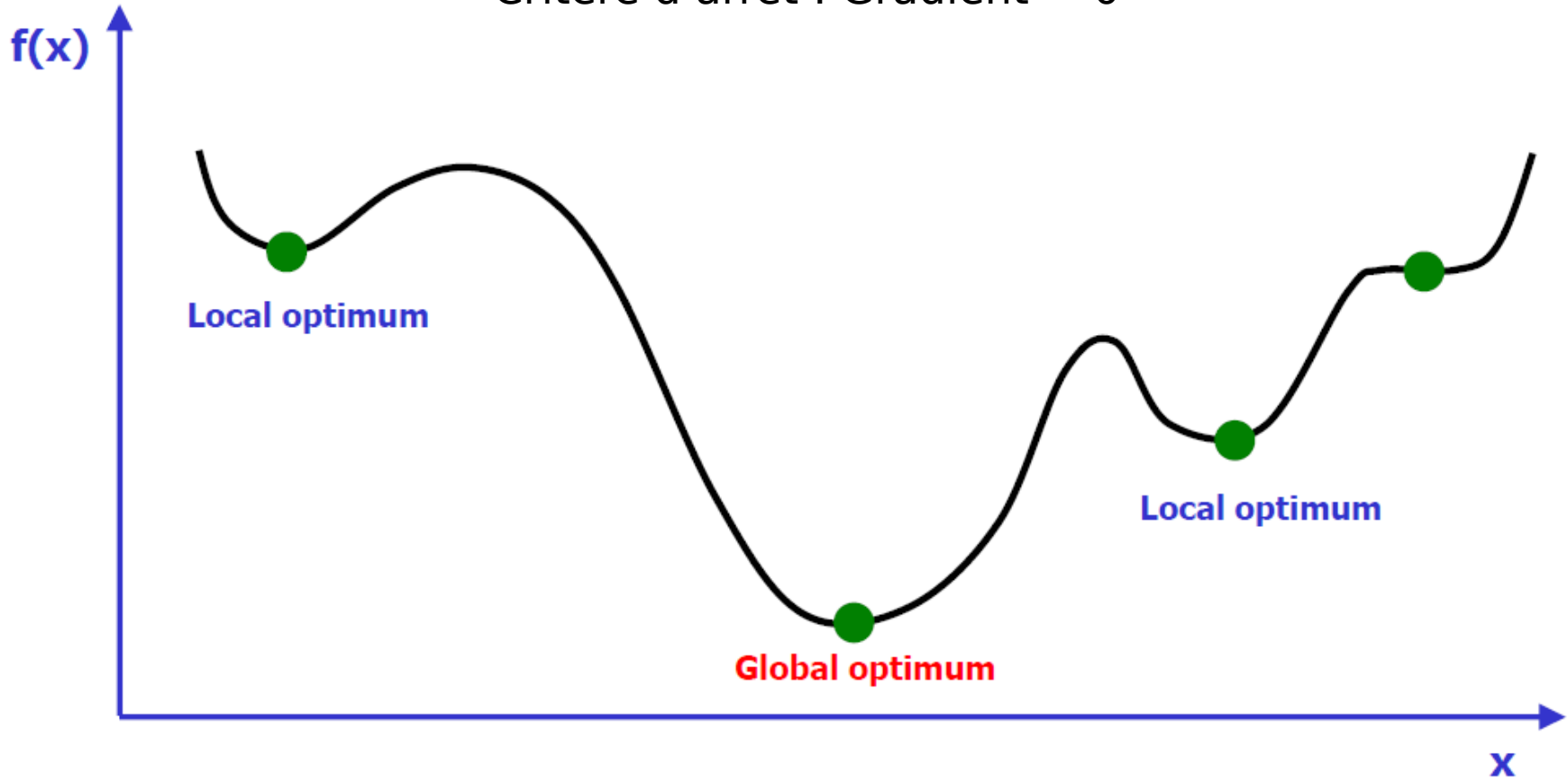


METHODES D'OPTIMISATION

METHODES BASEES SUR LE GRADIENT



Critère d'arrêt : Gradient = 0



No active constraints

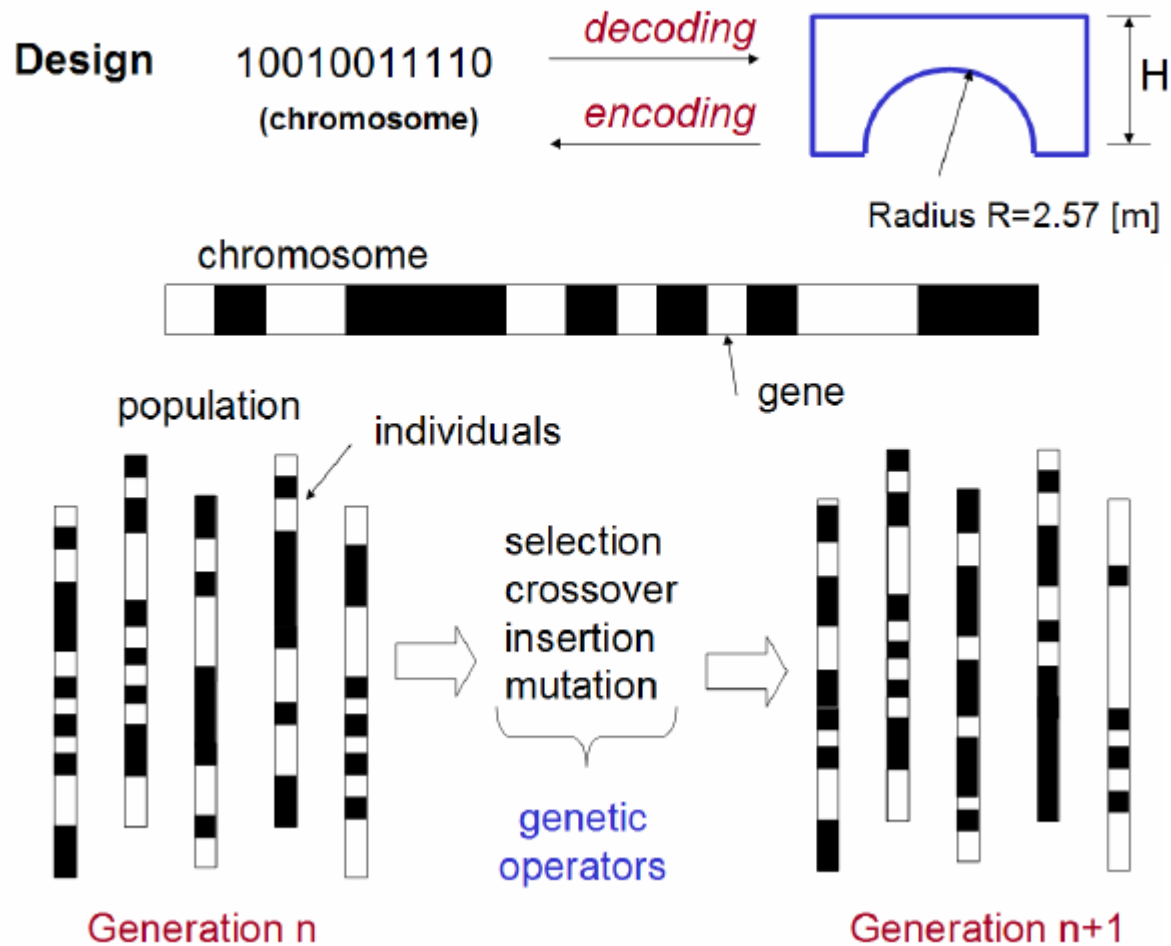


METHODES HEURISTICIS

- A **Heuristic** is simply a **rule of thumb** that hopefully will find a good answer.
- **Why** use a Heuristic?
 - Heuristics are typically used to solve **complex optimization problems** that are difficult to solve to optimality.
- Heuristics are **good at dealing with local optima** without getting stuck in them while searching for the global optimum.

LES ALGORITHMES GENETIQUES

Principle by Charles Darwin - Natural Selection





METHODES HEURISTICS

- Heuristics Often Incorporate Randomization
- **3 Most Common Heuristic Techniques**
 - Genetic Algorithms
 - Simulated Annealing
 - Tabu Search



❖ ANSYS



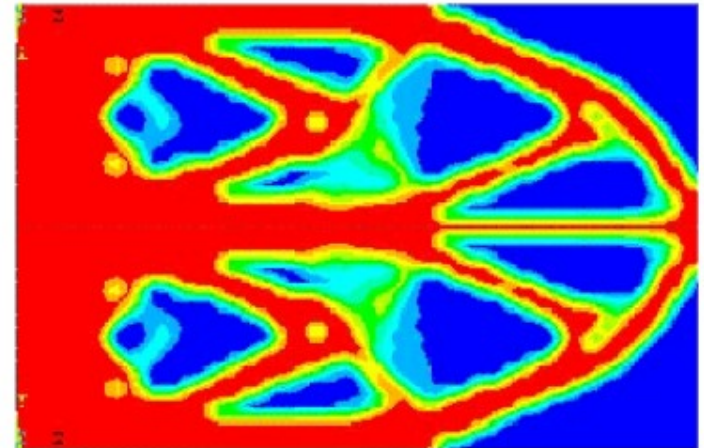
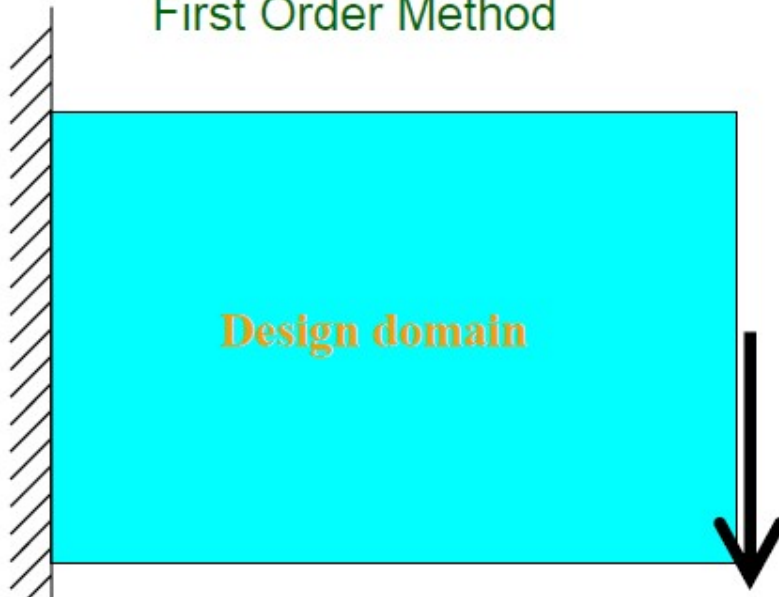
Static Topology Optimization

Dynamic Topology Optimization

Electromagnetic Topology Optimization

Subproblem Approximation Method

First Order Method





Multidisciplinary Design Optimization MDO

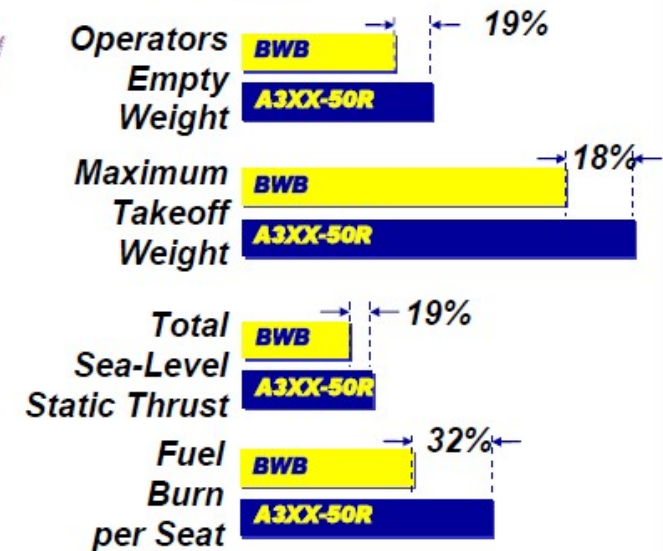
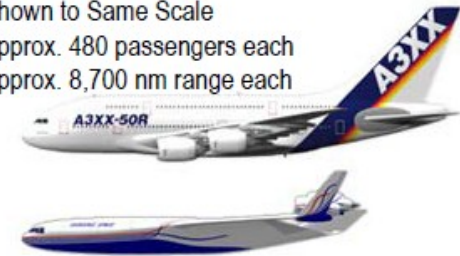
Boeing Blended Wing Body Concept



Goal: Find a design for a family of blended wing aircraft that will combine aerodynamics, structures, propulsion and controls such that a competitive system emerges - as measured by a set of operator metrics.

Aircraft Comparison

Shown to Same Scale
Approx. 480 passengers each
Approx. 8,700 nm range each



© Boeing

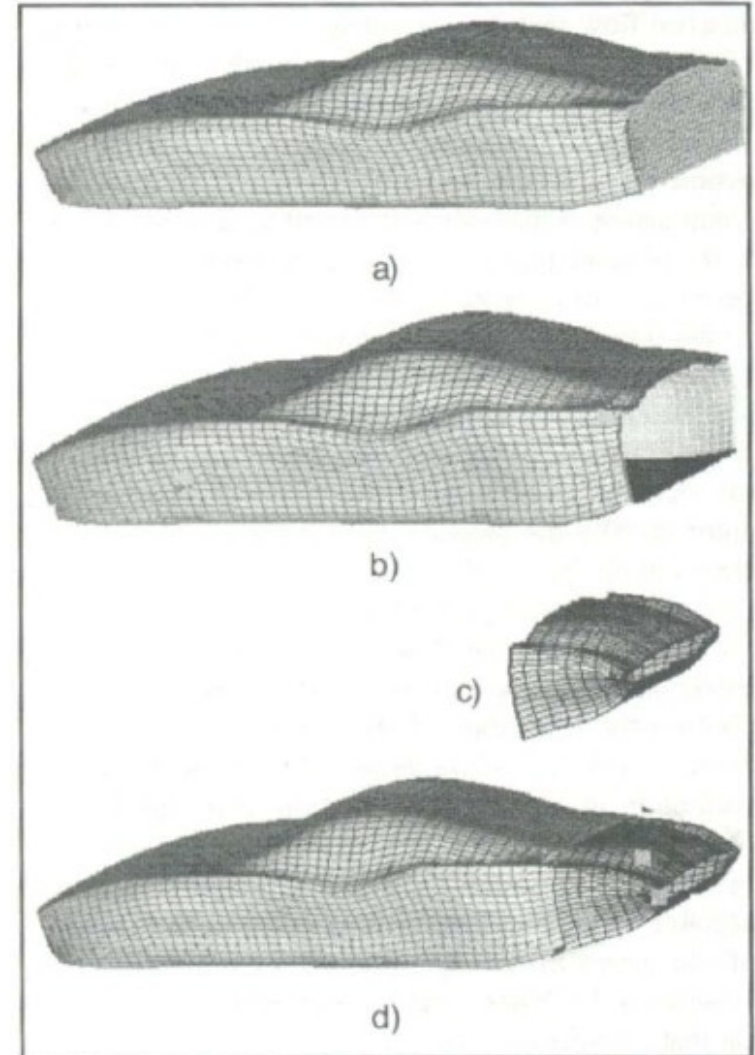
Multidisciplinary Design Optimization MDO

Ferrari 360 Spider



Goal: High end vehicle shape optimization while improving car safety for fixed performance level and given geometric constraints

Reference: G. Lombardi, A. Vicere, H. Paap, G. Manacorda,
"Optimized Aerodynamic Design for High Performance Cars", AIAA-98-4789, MAO Conference, St. Louis, 1998





Multidisciplinary Design Optimization MDO

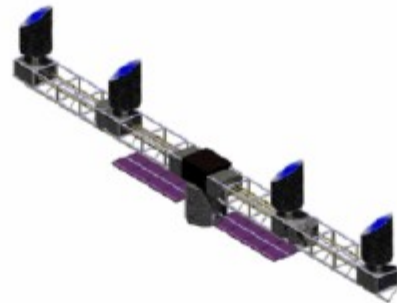
Aircraft:

Aerodynamics
Propulsion
Structures
Controls
Avionics/Software
Manufacturing
others



Spacecraft:

Astrodynamics
Thermodynamics
Communications
Payload & Sensor
Structures
Optics
Guidance & Control



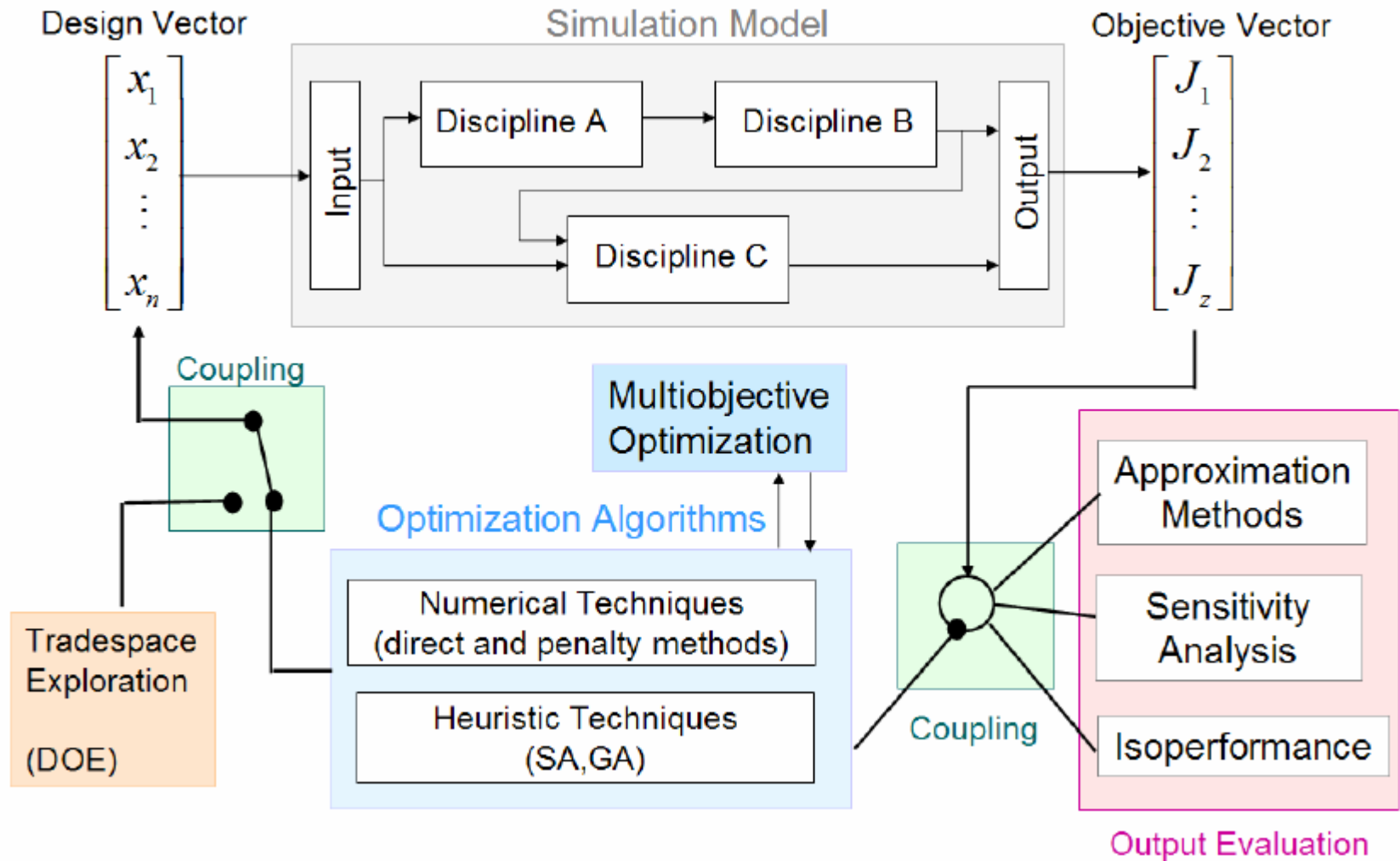
Automobiles:

Engines
Body/chassis
Aerodynamics
Electronics
Hydraulics
Industrial design
others



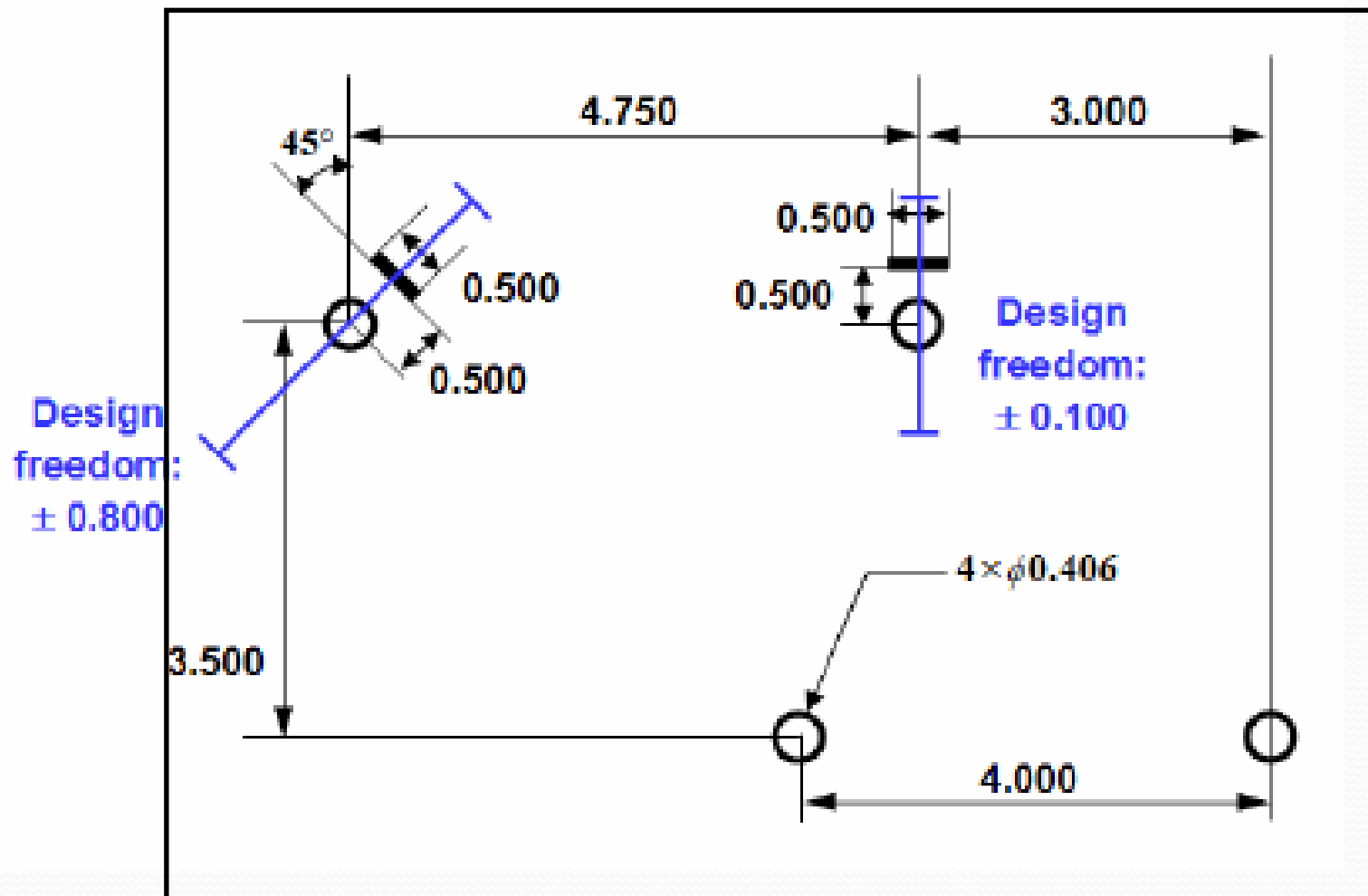


Multidisciplinary Design Optimization MDO

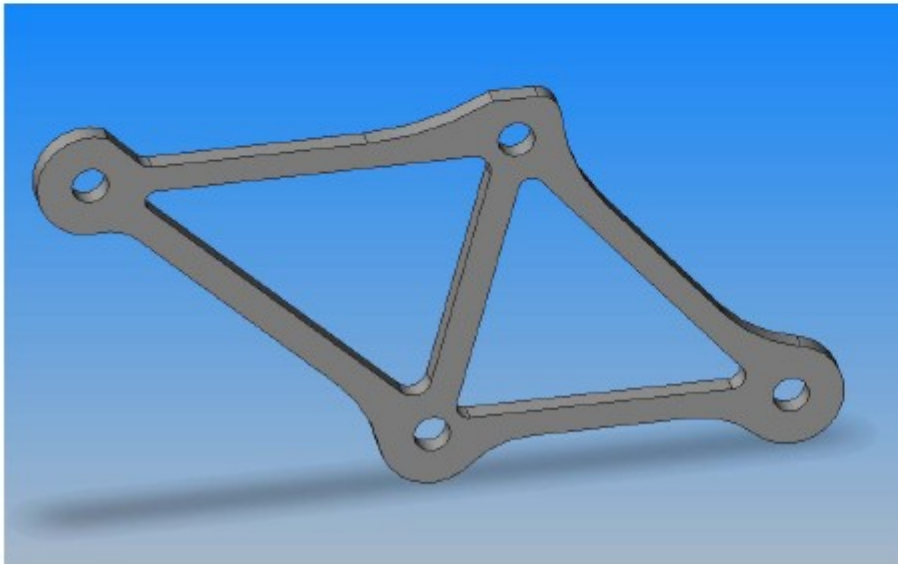
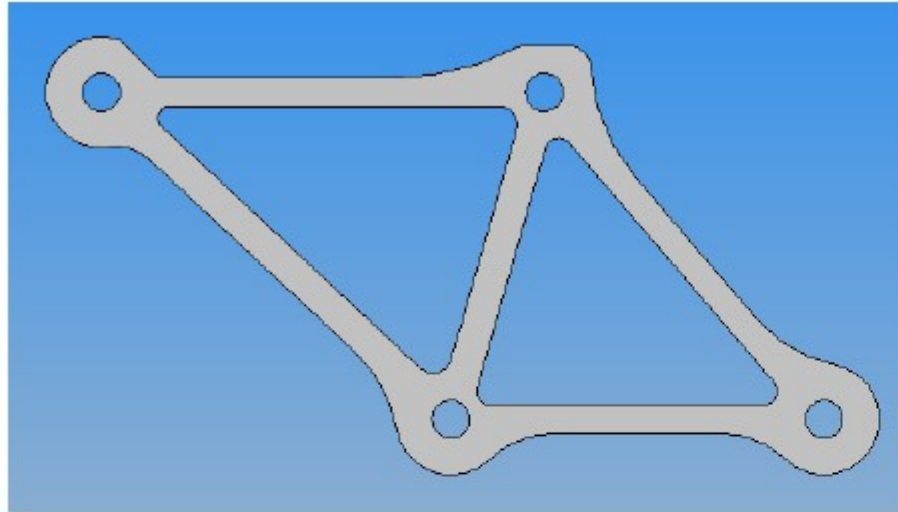




EXAMPLES



EXAMPLES



Performance and cost

$$\delta_1 = 0.070 \text{ mm}$$

$$\delta_2 = 0.011 \text{ mm}$$

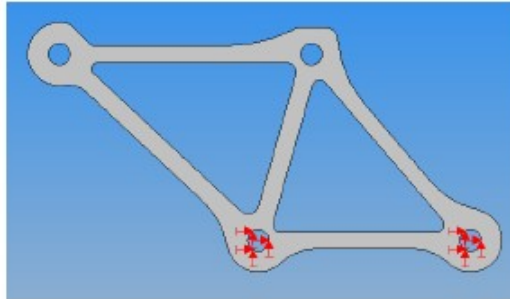
$$f = 245 \text{ Hz}$$

$$m = 0.224 \text{ lbs}$$

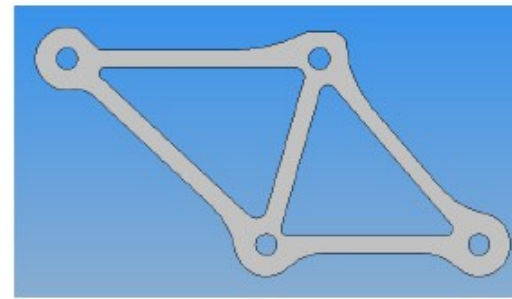
$$C = 5.16 \$$$

EXAMPLES

245 Hz



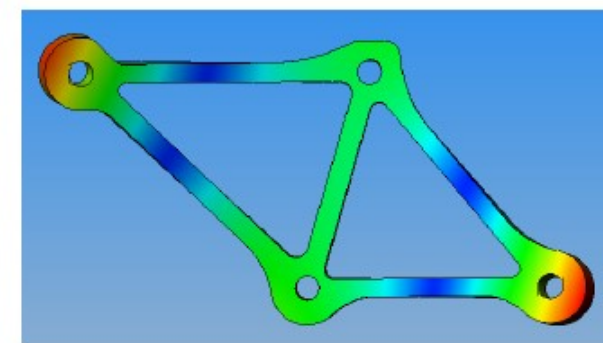
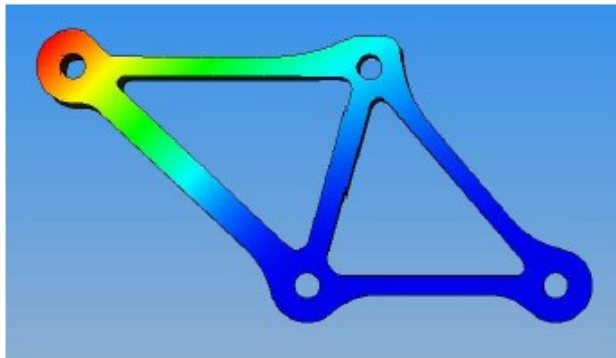
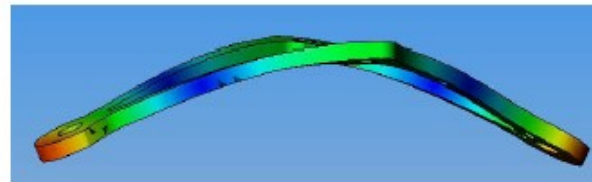
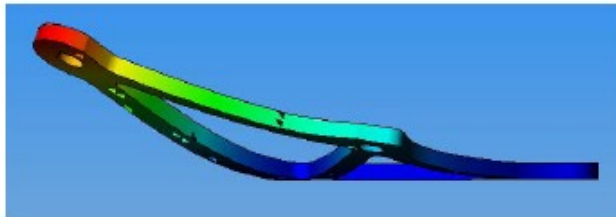
421 Hz



$f_1=245$ Hz

$f_2=490$ Hz

$f_3=1656$ Hz



$f_1=0$

$f_2=0$

$f_3=0$

$f_4=0$

$f_5=0$

$f_6=0$

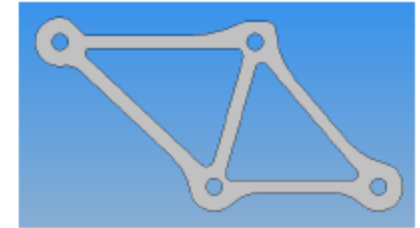
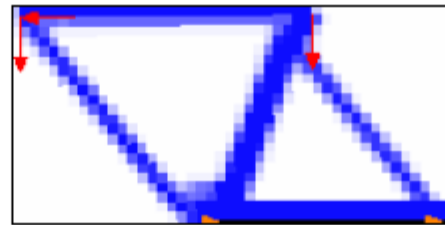
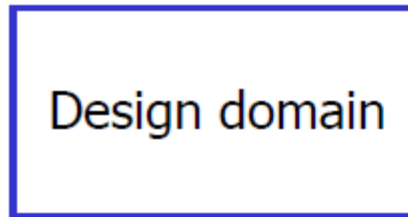
$f_7=421$ Hz

$f_8=1284$ Hz

$f_9=1310$ Hz

EXAMPLES

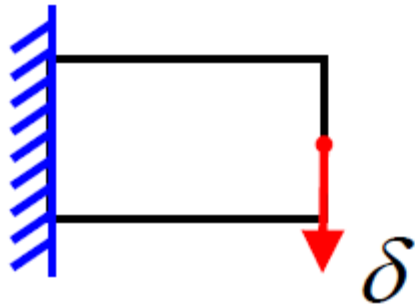
Topology optimization



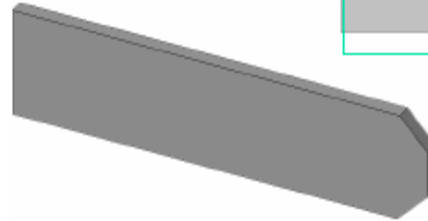
Shape optimization



EXAMPLES

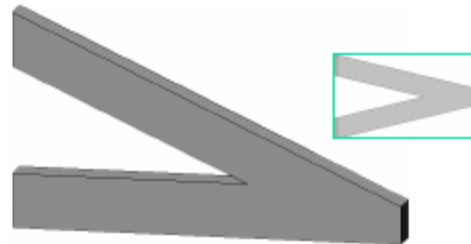


1 bar



$$\delta = 2.50 \text{ mm}$$

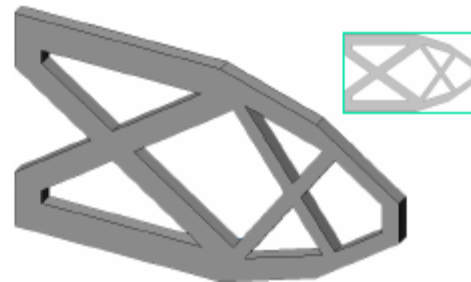
2 bars



$$\delta = 0.80 \text{ mm}$$

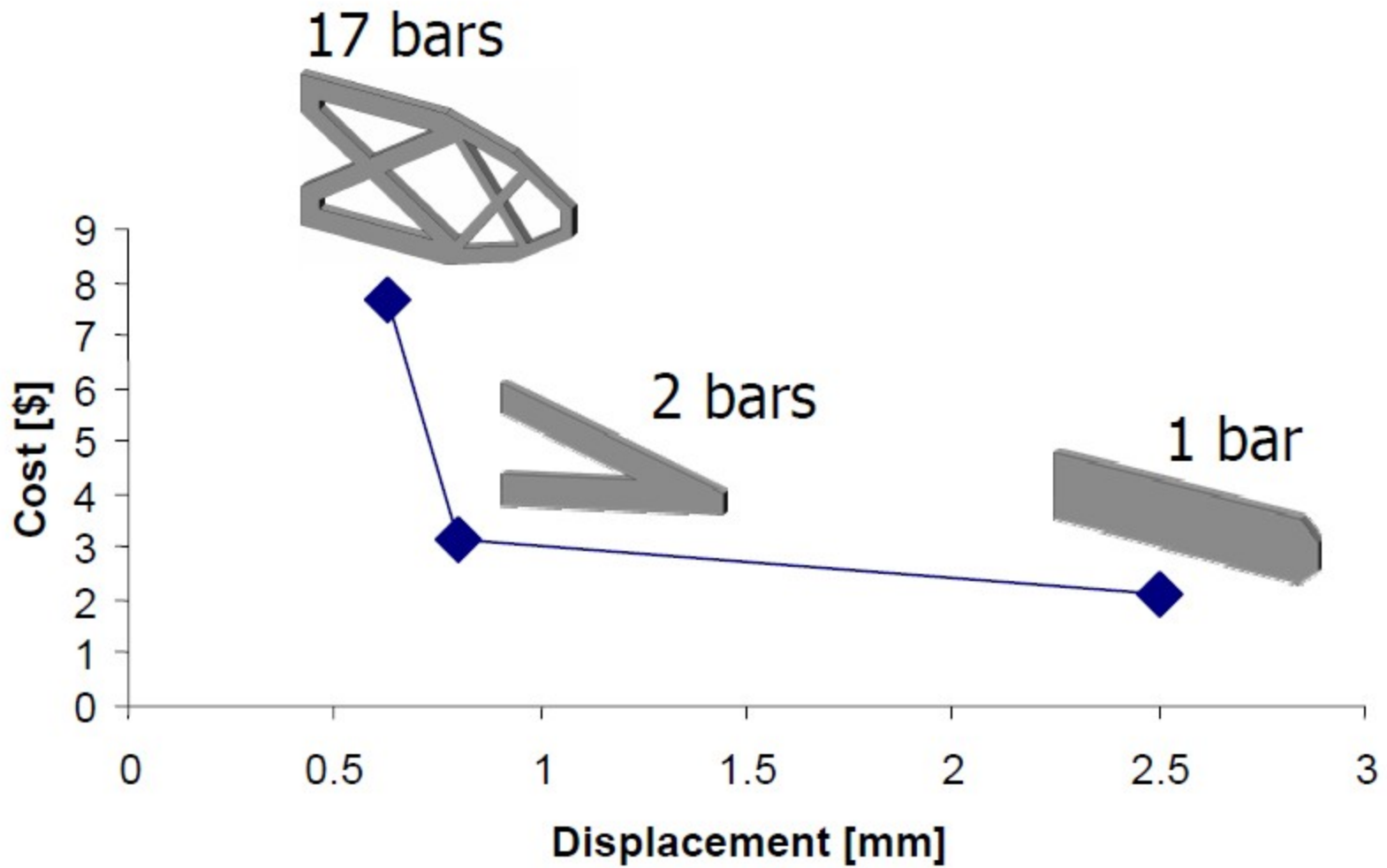
Volume is the same.

17 bars

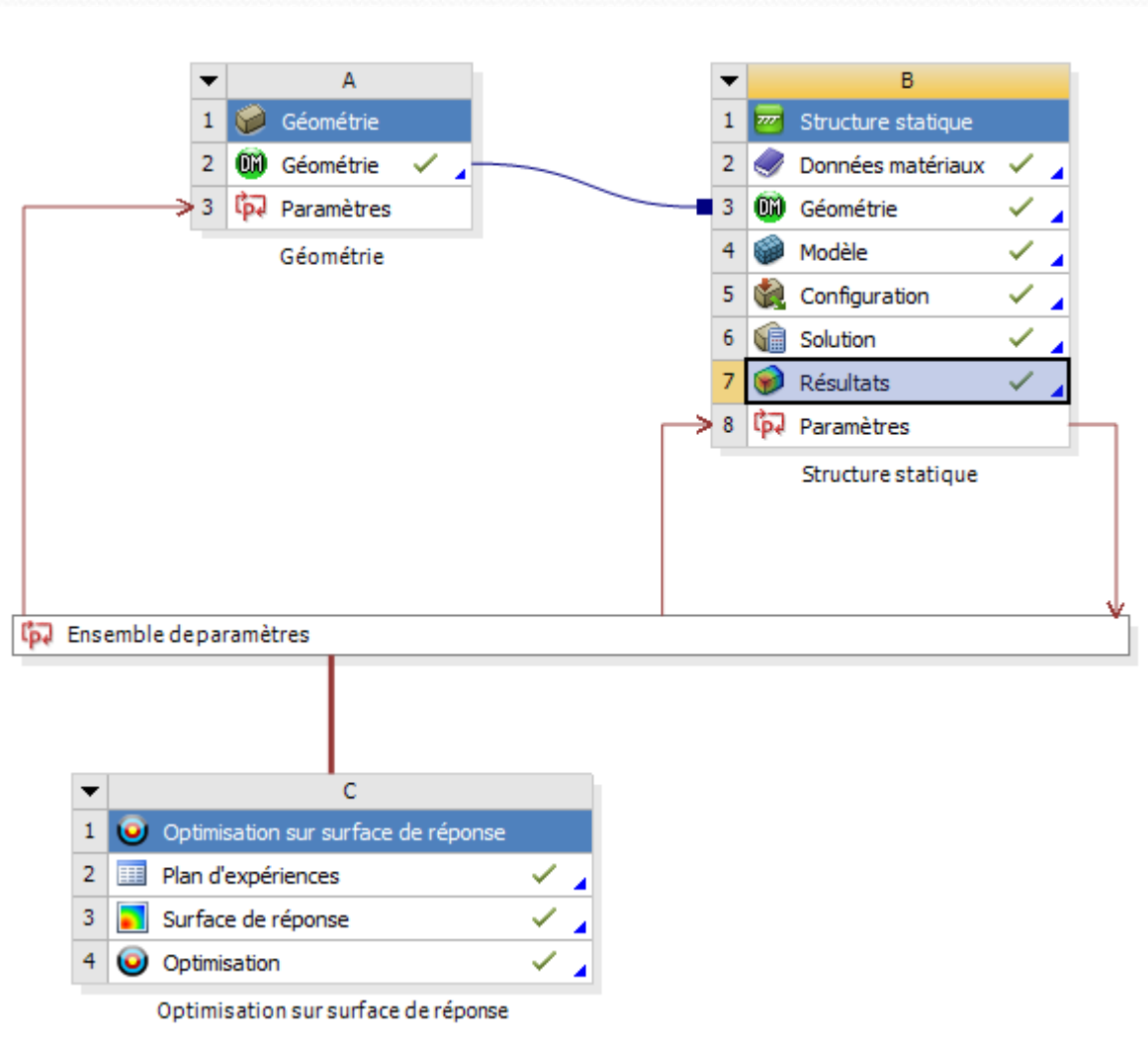
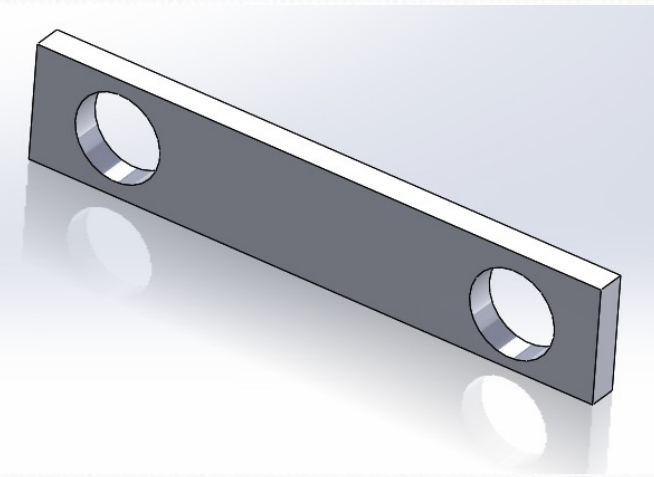


$$\delta = 0.63 \text{ mm}$$

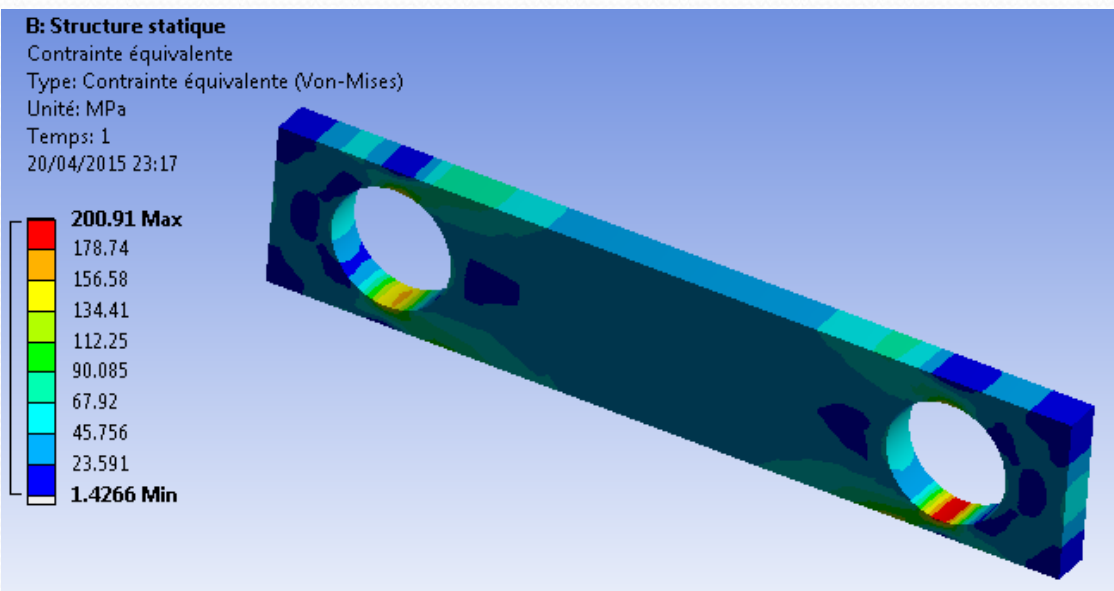
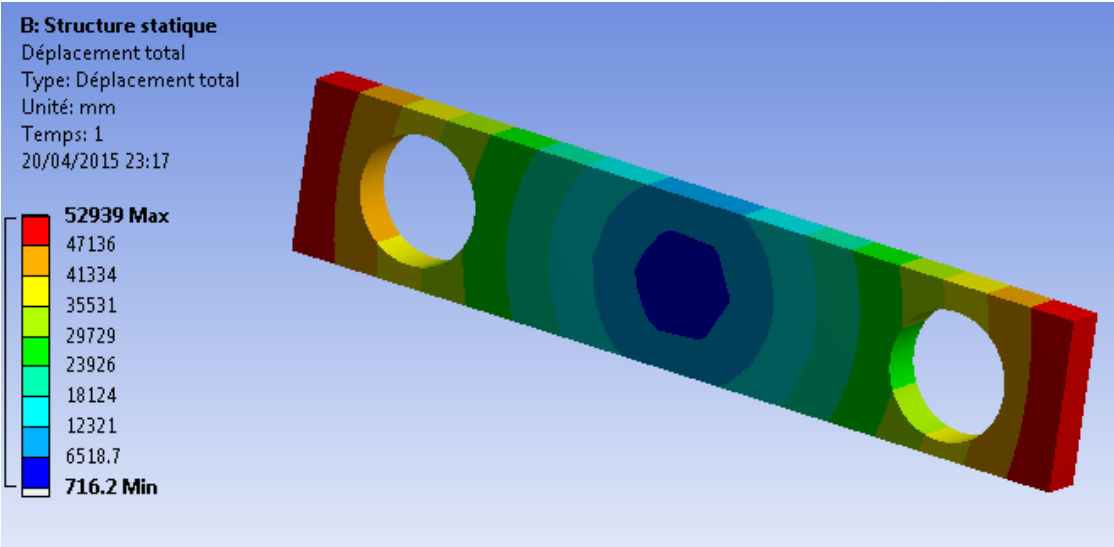
EXAMPLES



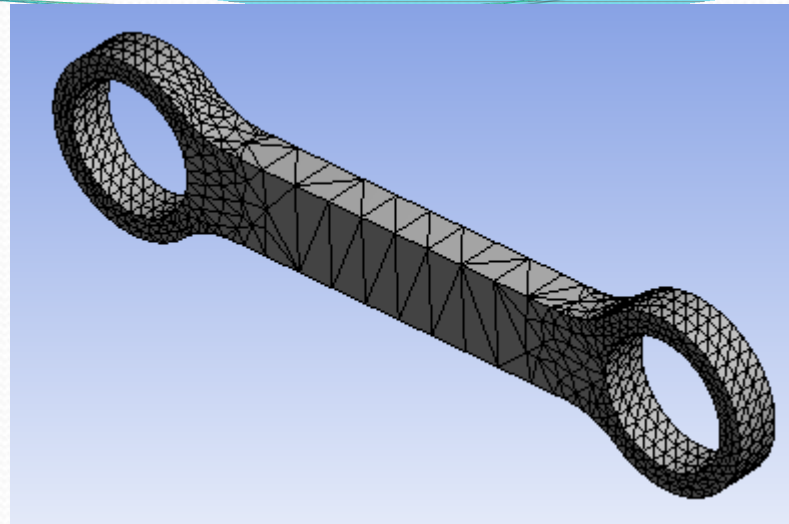
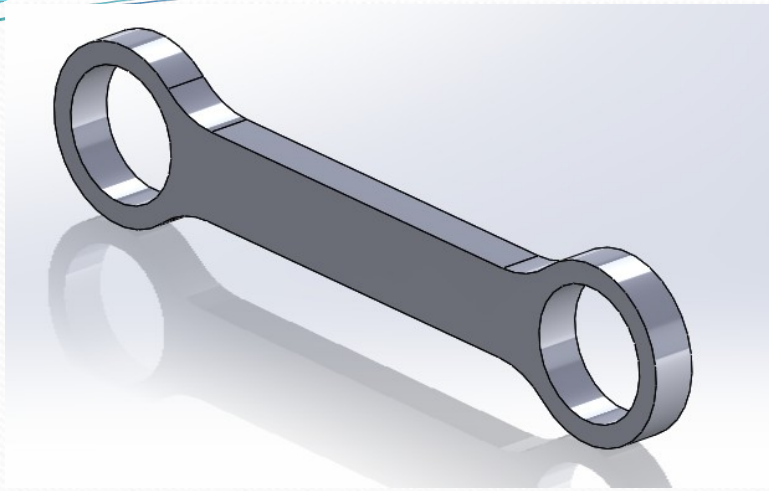
EXEMPLES



EXEMPLES

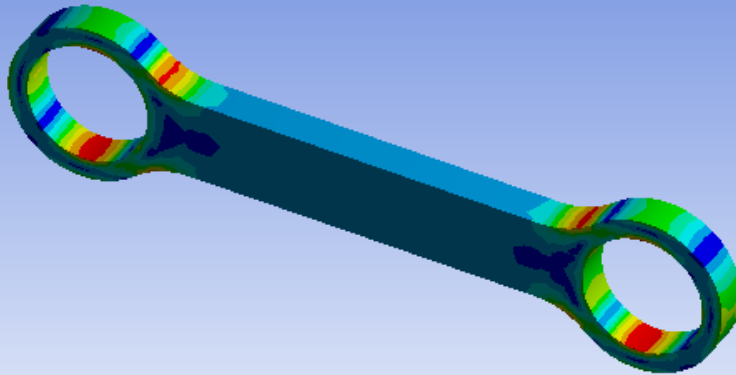
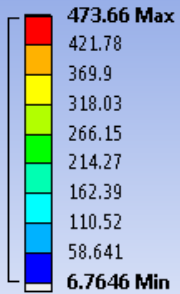


EXEMPLES



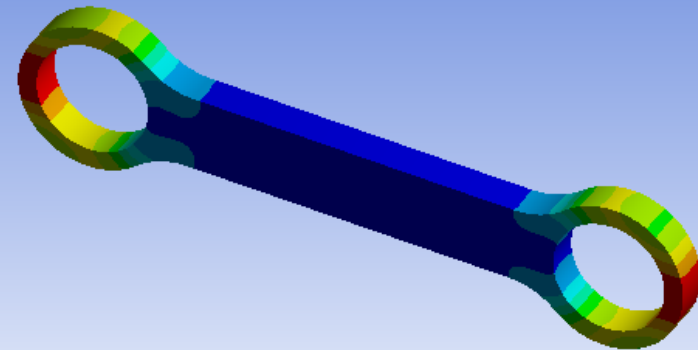
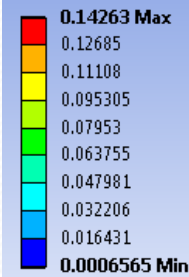
B: Structure statique

Contrainte équivalente
Type: Contrainte équivalente (Von-Mises)
Unité: MPa
Temps: 1
20/04/2015 23:22

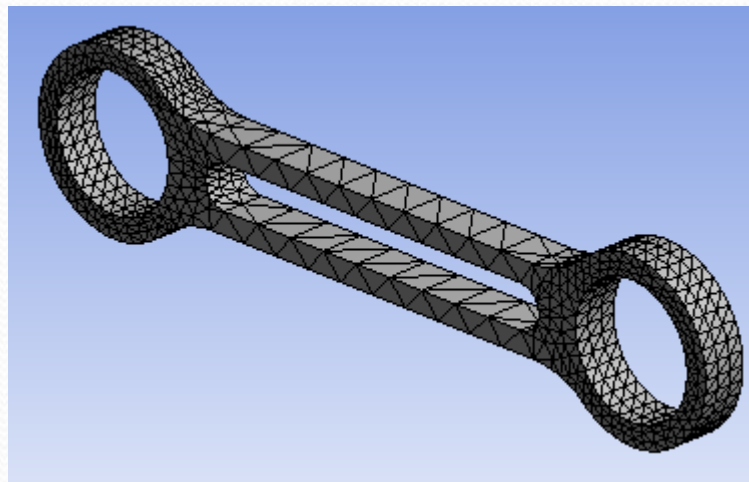
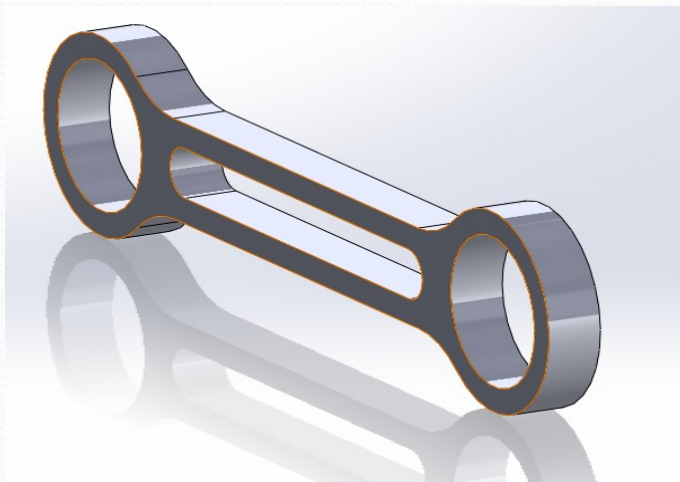


B: Structure statique

Déplacement total
Type: Déplacement total
Unité: mm
Temps: 1
20/04/2015 23:23



EXEMPLES



B: Structure statique

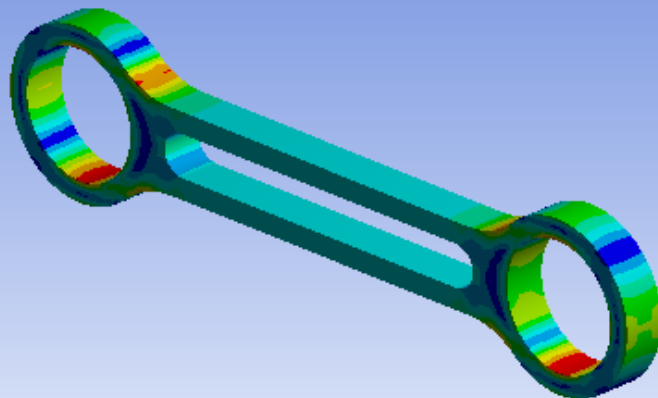
Contrainte équivalente

Type: Contrainte équivalente (Von-Mises)

Unité: MPa

Temps: 1

20/04/2015 23:24



478.83 Max

426.32

373.82

321.31

268.81

216.3

163.8

111.29

58.788

6.2836 Min

B: Structure statique

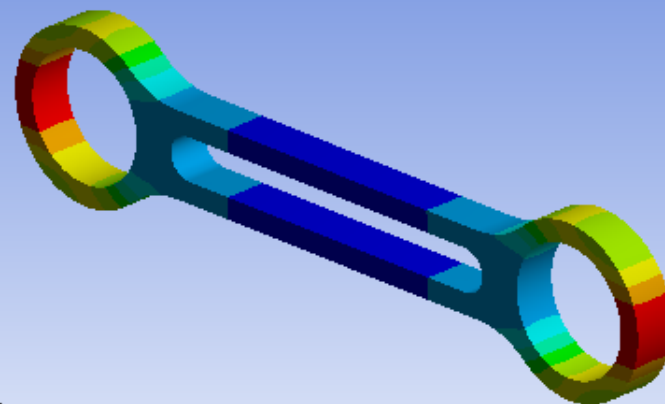
Déplacement total

Type: Déplacement total

Unité: mm

Temps: 1

20/04/2015 23:24



0.16004 Max

0.14279

0.12555

0.10831

0.091062

0.073818

0.056574

0.03933

0.022086

0.0048416 Min

EXEMPLES



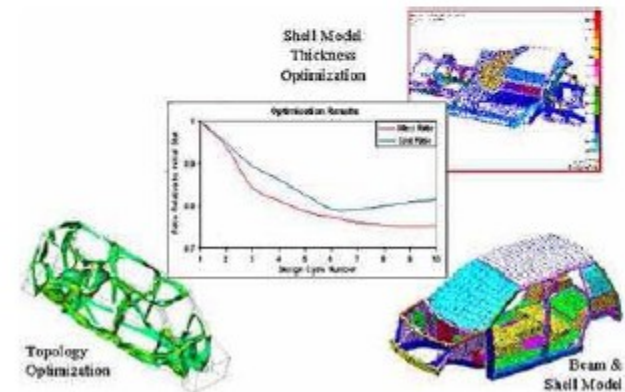
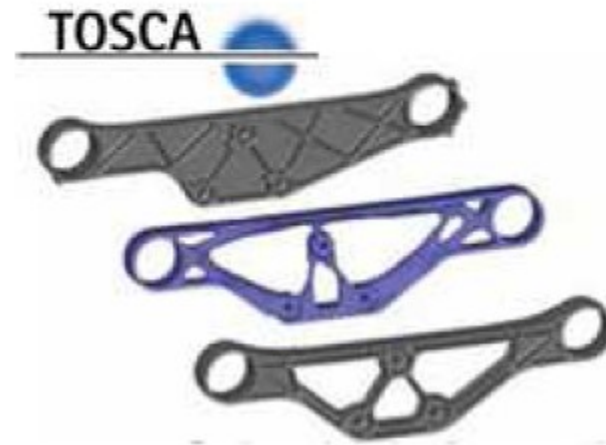
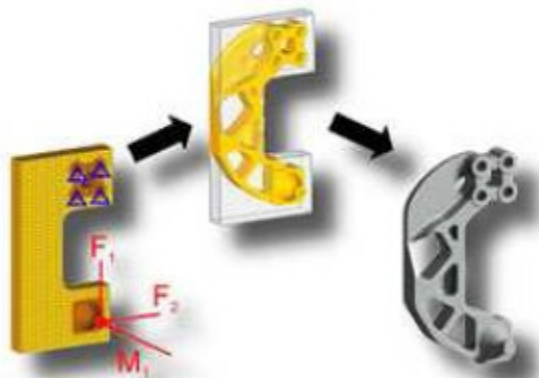
EXEMPLES



EXEMPLES

Logiciels industriels

Optistruct, Ansys DesignSpace, Genesis, MSC-Nastran, Tosca, devDept...





MERC

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Pr. BOUDI M.
EMI